

Resolving Stress Components and Earthquake Triggering

*Last updated:
4 February 2020*

Earthquake Triggering

- Do certain events make an earthquake more likely to occur?

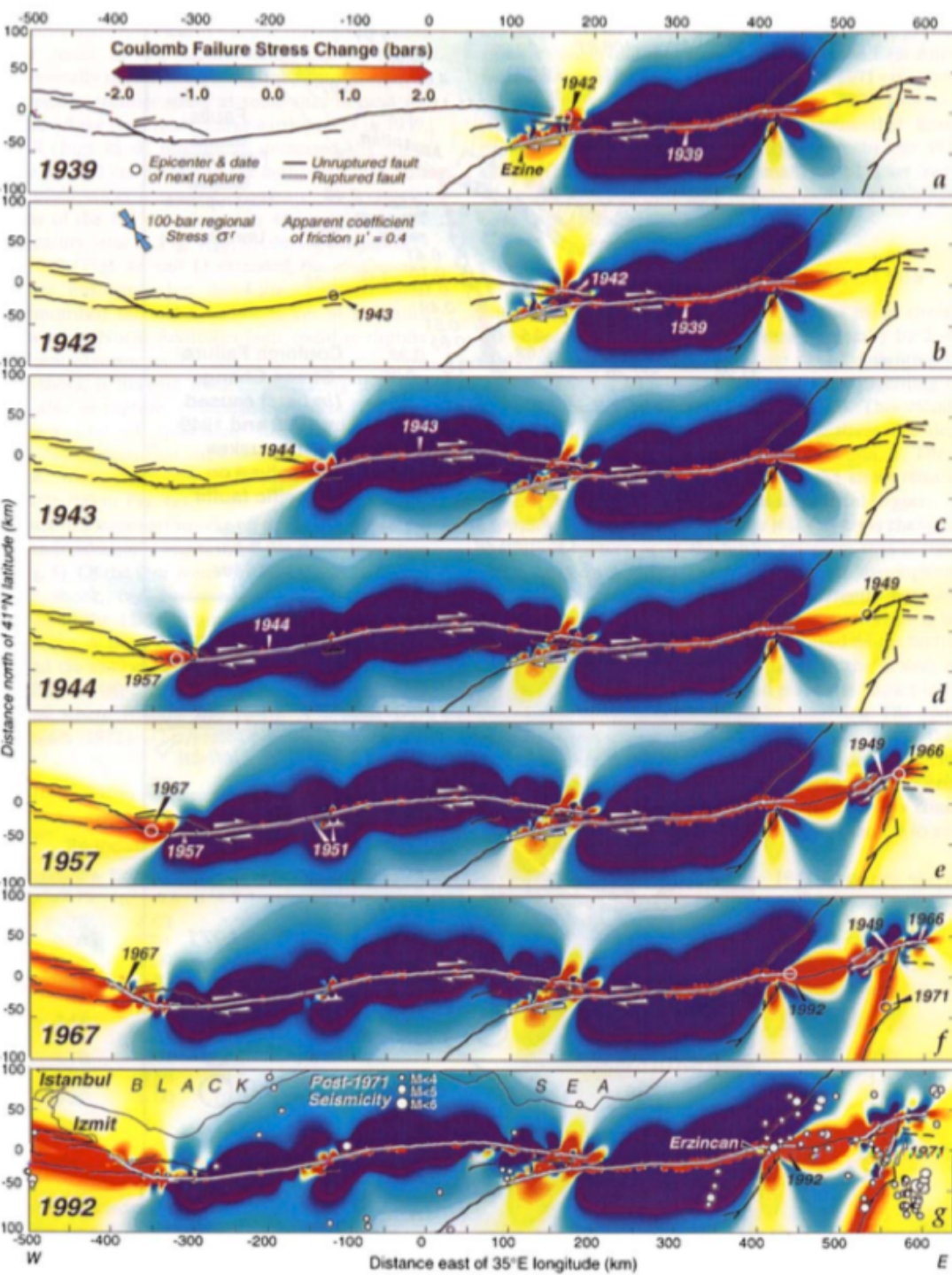
- Earthquakes

*The focus of this
presentation*

- Slow Slip

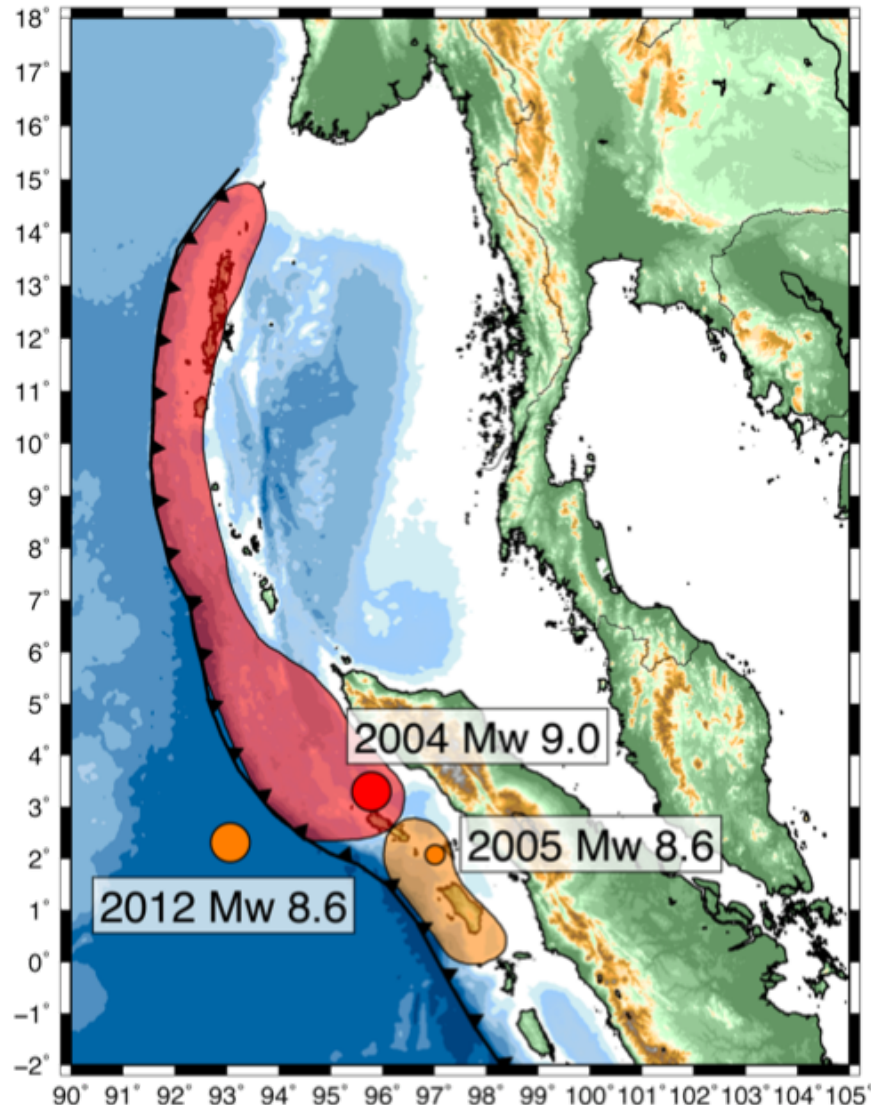
- Wastewater Fluids

- Dams



- 20th century earthquakes on the N. Anatolian Fault in Turkey progressed systematically westward
- Stein et al. (1997): Each event triggered by the previous

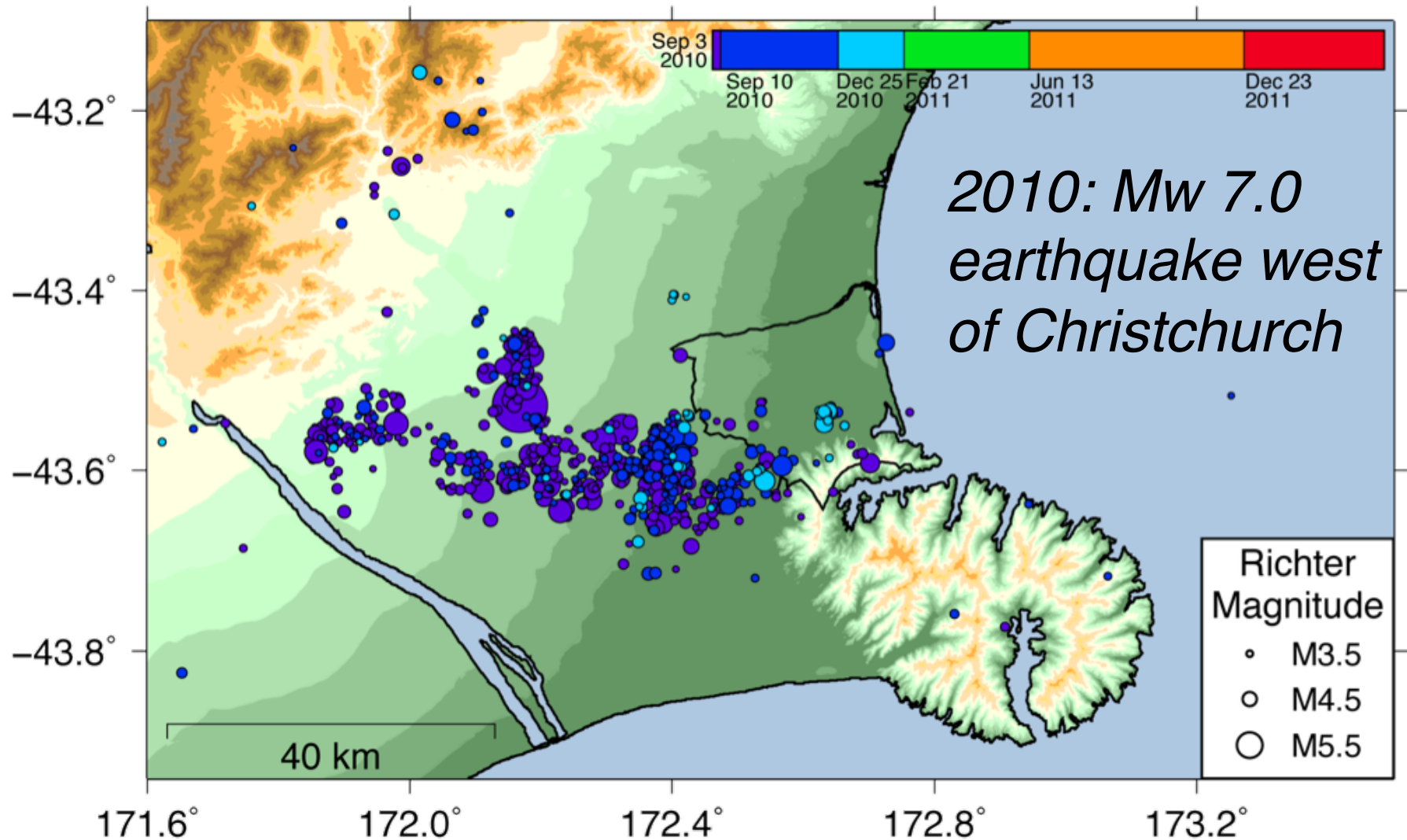
Earthquake Triggering



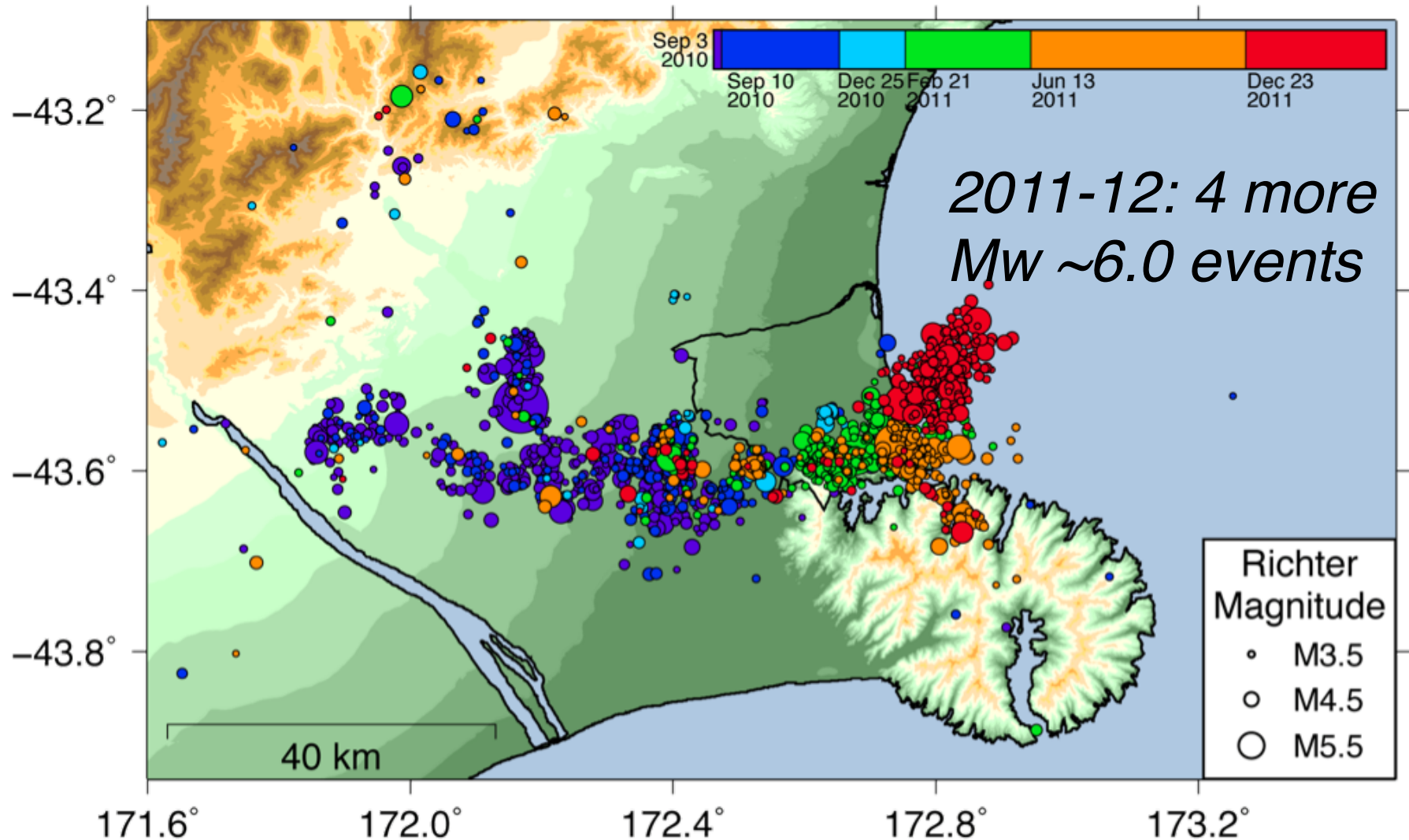
- 2004 Mw 9.0 Sumatra-Andaman earthquake
- 2005 Mw 8.6 earthquake to south
- 2012 Mw 8.6 strike-slip earthquake outboard of trench

Rupture areas: *USGS Seismicity of the Earth 1900-2012: Sumatra and Vicinity*

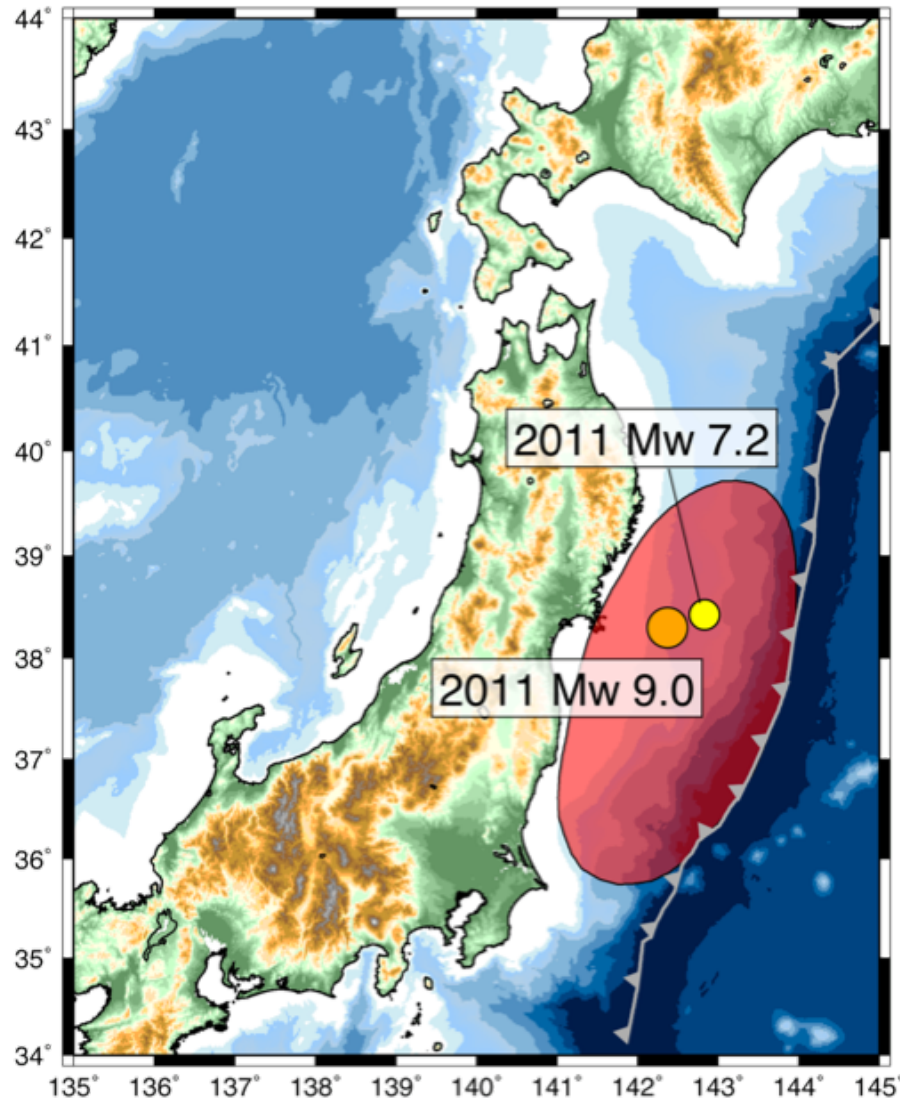
Earthquake Triggering



Earthquake Triggering



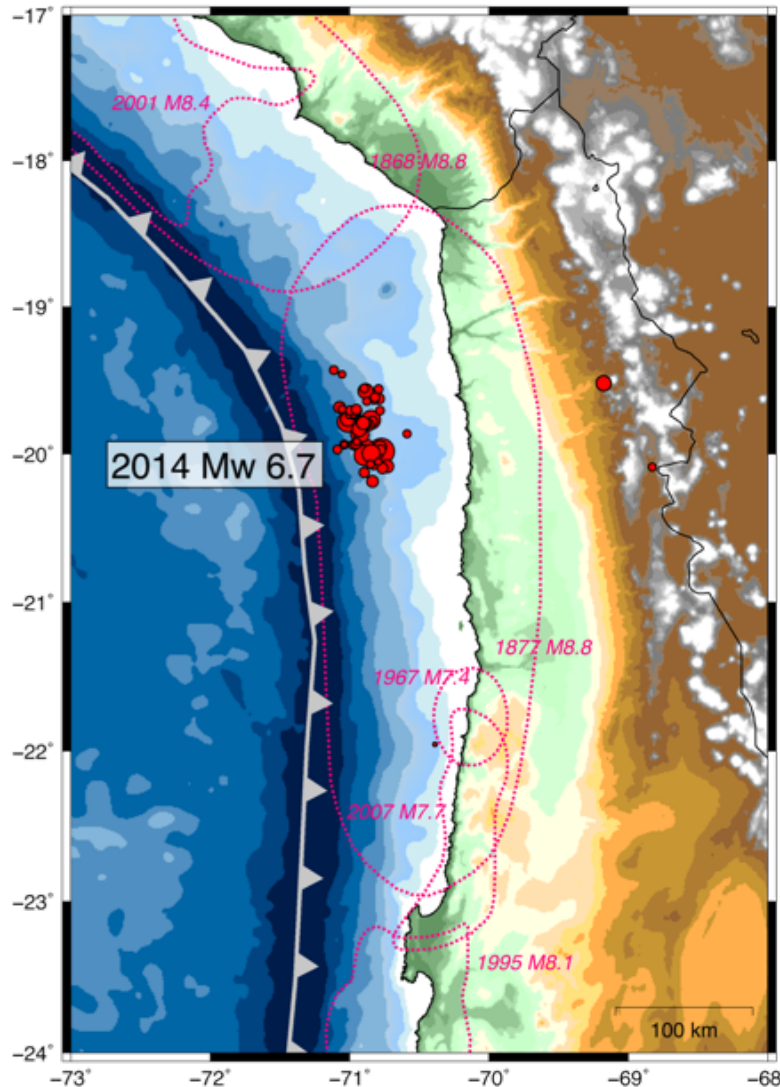
Earthquake Triggering



- 2011 Mw 7.2 earthquake offshore Honshu
- Two days later, great Mw 9.0 Tohoku-oki earthquake

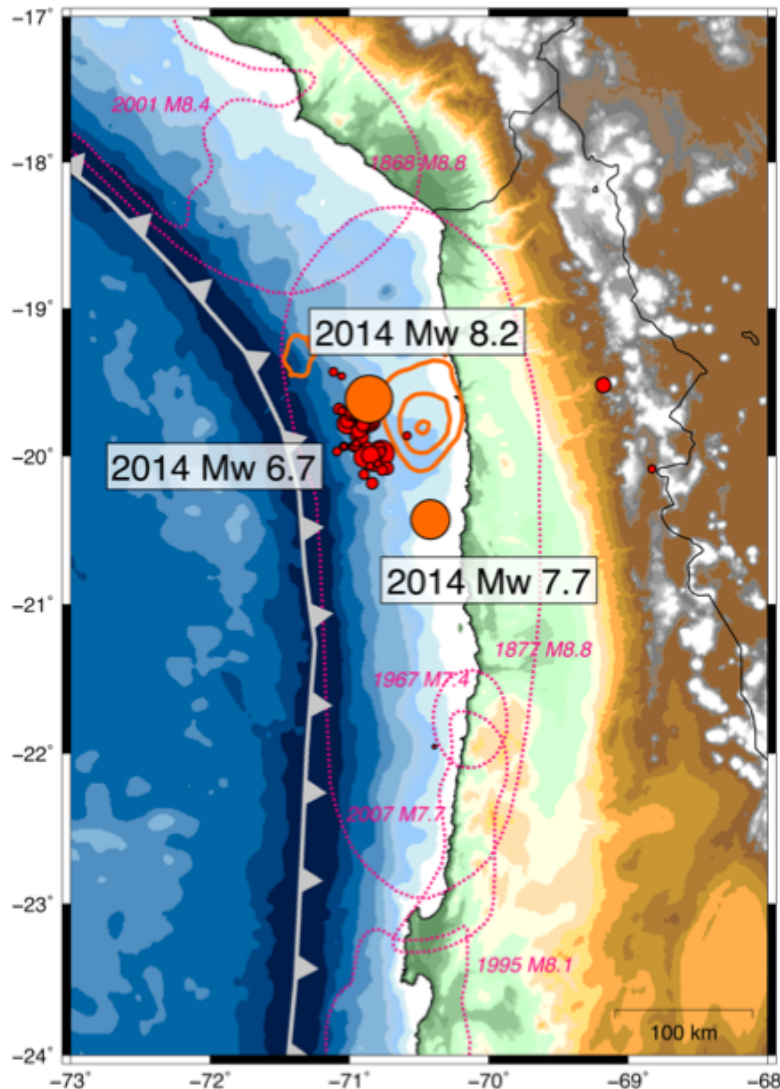
Rupture area: *Ozawa et al. (2011)*

Earthquake Triggering



- March 2014: offshore N. Chile earthquake sequence starts with Mw 6.7

Earthquake Triggering



- March 2014: offshore N. Chile earthquake sequence starts with Mw 6.7
- 1 April 2014: Mw 8.2 Iquique earthquake, followed on 3 April by Mw 7.7 aftershock

Resolving Stresses

- Recall from earlier: stress tensor
- For simplicity, we will do the following derivations in 2-D, but all of this math can be extended to 3-D (and is in O92UTIL)

$$\sigma = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{bmatrix} \Rightarrow \sigma = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{bmatrix}$$

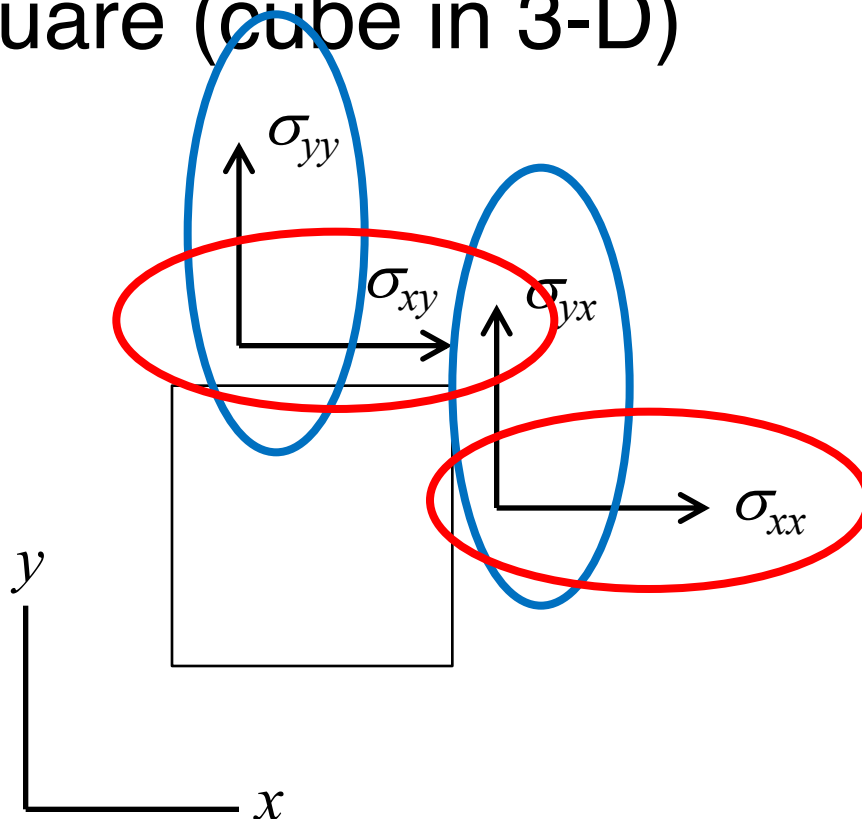
Resolving Stresses

- Stress tensor represents tractions on an infinitesimal square (cube in 3-D)

$$\sigma = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{bmatrix}$$

X-tractions

Y-tractions



Resolving Stresses

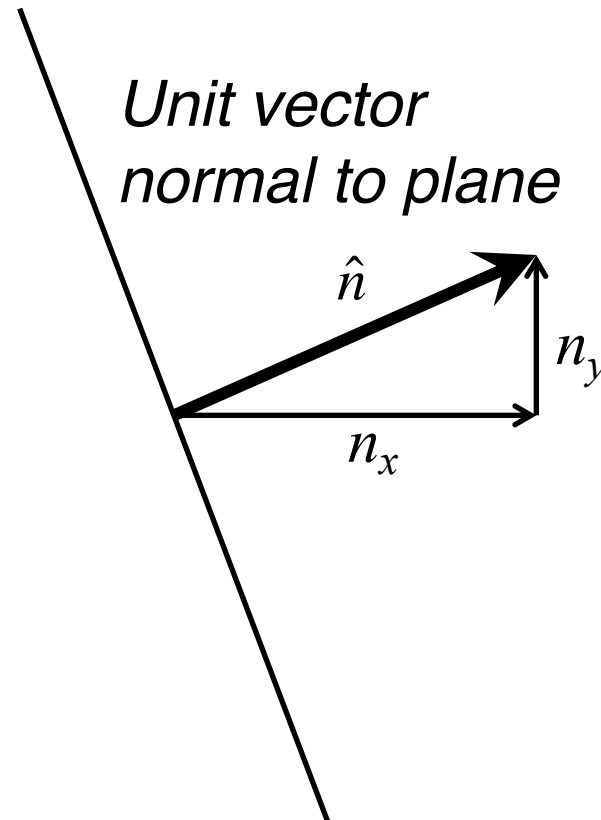
- What about the tractions on an arbitrarily oriented plane?

$$\sigma = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{bmatrix}$$

$$t_x = \sigma_{xx}n_x + \sigma_{xy}n_y$$

$$t_y = \sigma_{yx}n_x + \sigma_{yy}n_y$$

Matrix equation!



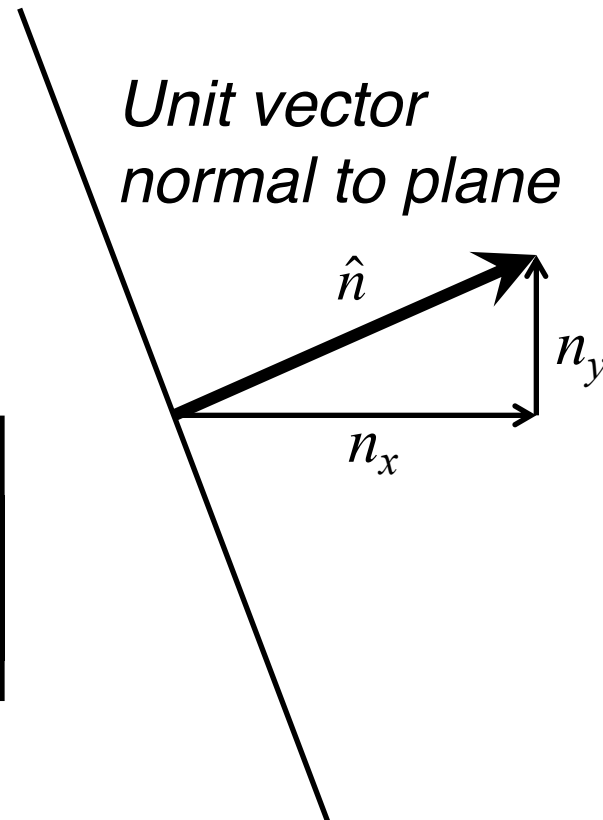
Resolving Stresses

- What about the tractions on an arbitrarily oriented plane?

$$\sigma = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{bmatrix}$$

$$\begin{bmatrix} t_x \\ t_y \end{bmatrix} = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{bmatrix} \begin{bmatrix} n_x \\ n_y \end{bmatrix}$$

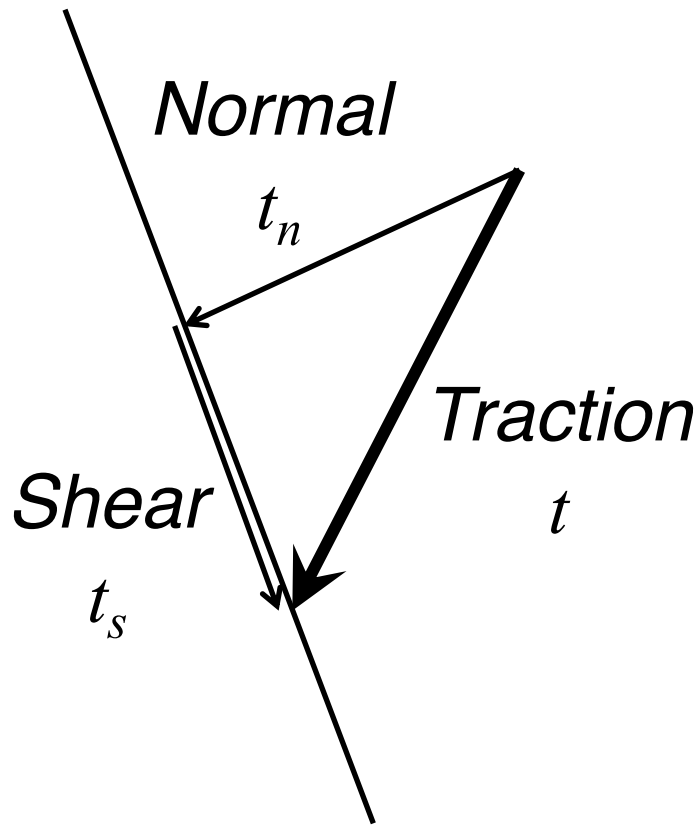
$$\vec{t} = \sigma \hat{n}$$



Resolving Stresses

- Earthquakes occur when the *shear stress* on the fault surface is greater than the frictional resistance (friction coefficient times *normal stress*)
- The traction vector can be divided into shear and normal components

Resolving Stresses



$$\vec{t} = \sigma \hat{n}$$

For the normal component of traction, compute the dot product with the unit normal:

$$t_n = \vec{t} \cdot \hat{n}$$

The shear component is the difference between the traction vector and the normal component:

$$\vec{t}_s = \vec{t} - t_n \hat{n}$$

Resolving Stresses

- O92UTIL computes these quantities from the stresses generated by a slipping fault and can output either shear or normal stress components, or both
- *Requires target (or “receiver”) fault geometry!*

Resolving Stresses

- Shear and normal stress commonly combined into *Coulomb stress change* (ΔCS)

$$\Delta CS = \tau - \mu \sigma_n$$

- If ΔCS is positive, fault is brought closer to failure
- If ΔCS is negative, fault is inhibited from failure

Modeling Overview

INPUTS

Faults

Receivers

Elastic properties

Target faults*

OUTPUTS

Displacement

Strain tensor

Stress tensor

Normal stress*

Shear stress*

Coulomb stress*

**To resolve stresses on planes in the subsurface, must define target fault orientations*

Modeling Overview

INPUTS

Faults

Receivers

Elastic properties

Target faults*

*Now we need target
fault geometries to
resolve stresses on.*

OUTPUTS

Displacement

Strain tensor

Stress tensor

Normal stress*

Shear stress*

Coulomb stress*

**To resolve stresses on planes in the subsurface, must define target fault orientations*

Modeling Overview

INPUTS

Faults

Receivers

Elastic properties

Target faults*

OUTPUTS

We will focus on Coulomb stress, but recall it is derived from normal and shear stresses.

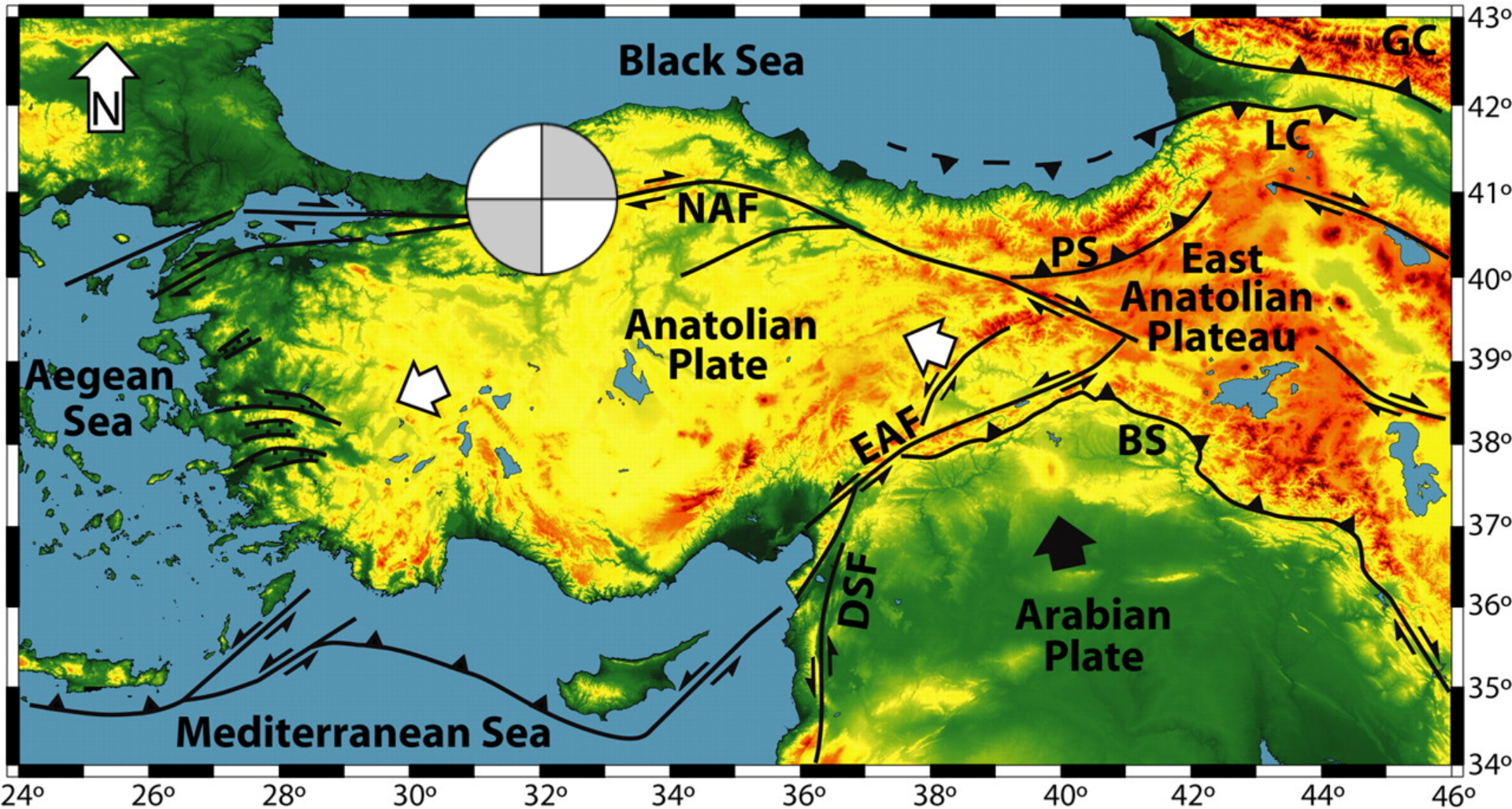
Normal stress*

Shear stress*

Coulomb stress*

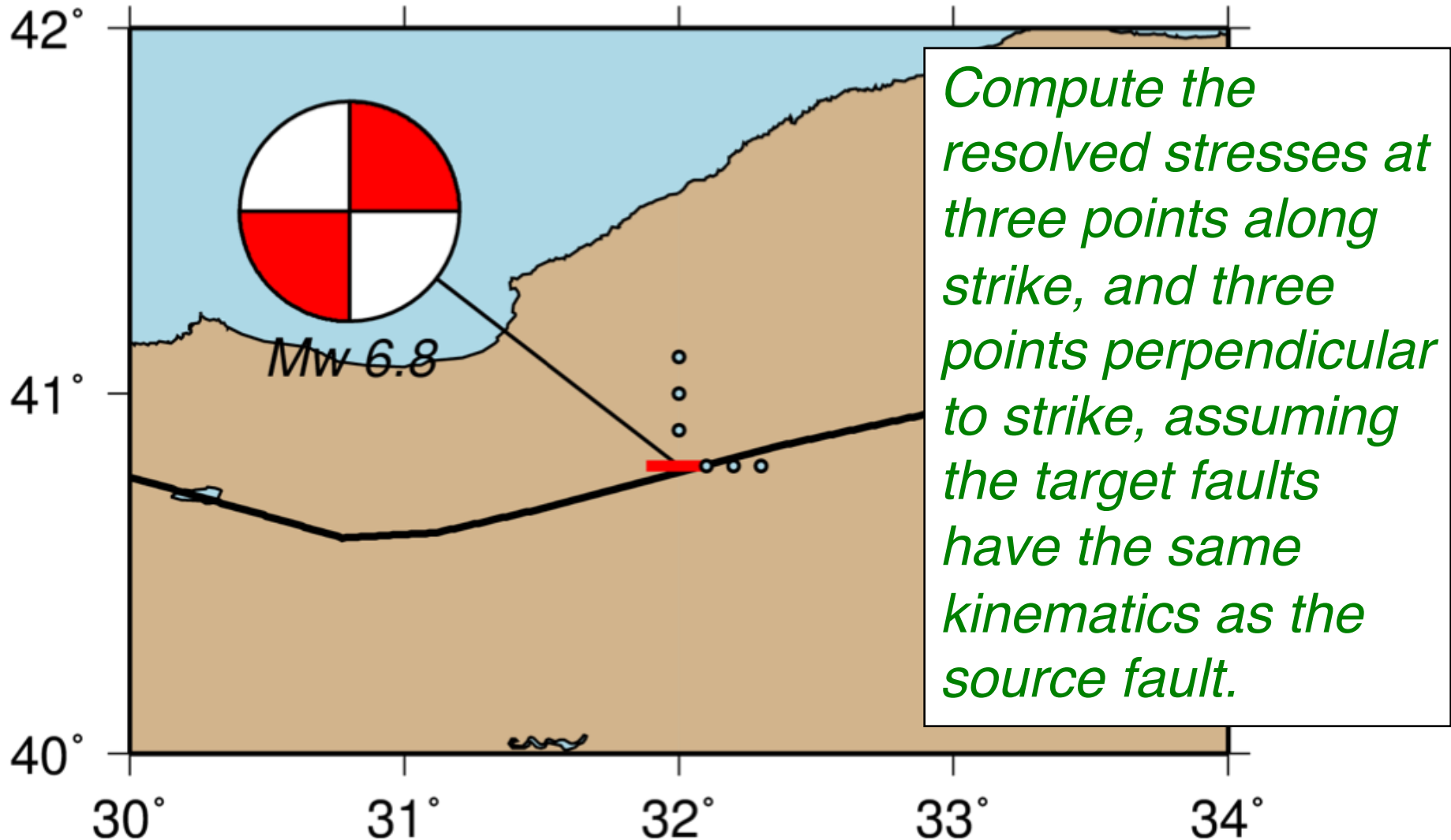
**To resolve stresses on planes in the subsurface, must define target fault orientations*

Activity 1: Strike-Slip Event



Hypothetical Mw 6.8 on the North Anatolian Fault, Turkey

Activity 1: Strike-Slip Event

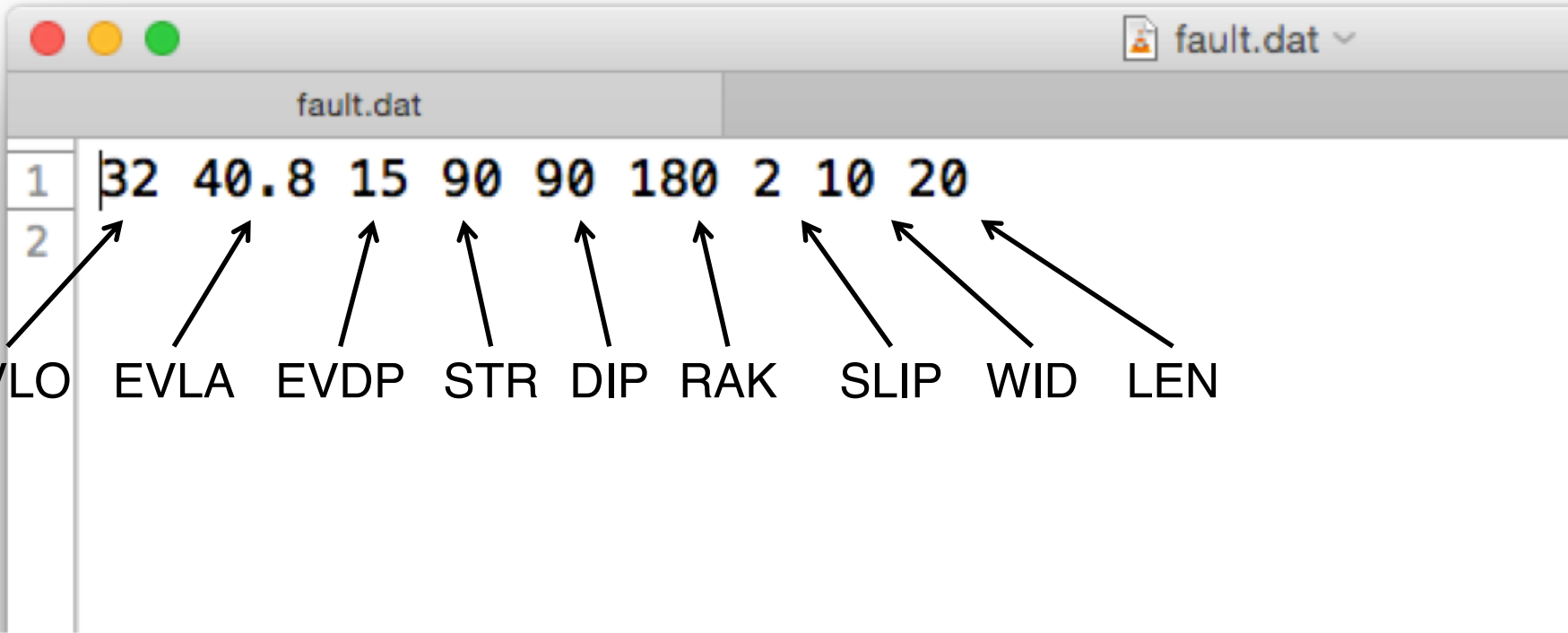


Activity 1: Strike-Slip Event

- Input files
 - Fault file (fault.dat)

Activity 1: Strike-Slip Event

- fault.dat



A screenshot of a file editor window titled "fault.dat". The window displays a single line of data: "32 40.8 15 90 90 180 2 10 20". Below the data, there are nine labels: "EVLO", "EVLA", "EVDP", "STR", "DIP", "RAK", "SLIP", "WID", and "LEN". Arrows point from each label to its corresponding value in the data row: EVLO to 32, EVLA to 40.8, EVDP to 15, STR to 90, DIP to 90, RAK to 180, SLIP to 2, WID to 10, and LEN to 20.

	32	40.8	15	90	90	180	2	10	20
1									
2									

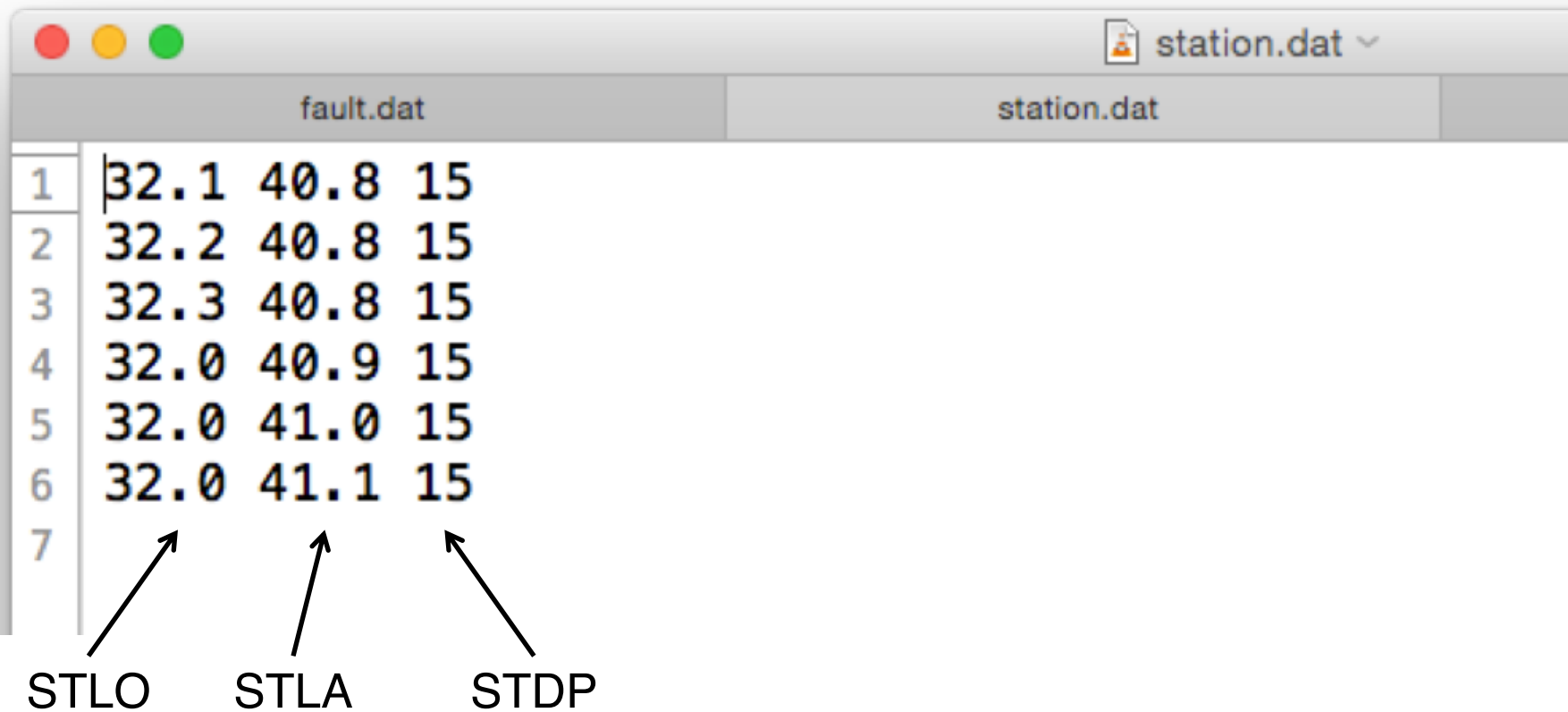
EVLO EVLA EVDP STR DIP RAK SLIP WID LEN

Activity 1: Strike-Slip Event

- Input files
 - Fault file (fault.dat)
 - Receiver locations (station.dat)

Activity 1: Strike-Slip Event

- station.dat



A screenshot of a file editor window titled 'station.dat'. The window displays a table with 7 rows and 3 columns. The columns are labeled 'STLO', 'STLA', and 'STDP' at the bottom, with arrows pointing to the corresponding columns in the table. The data in the table is as follows:

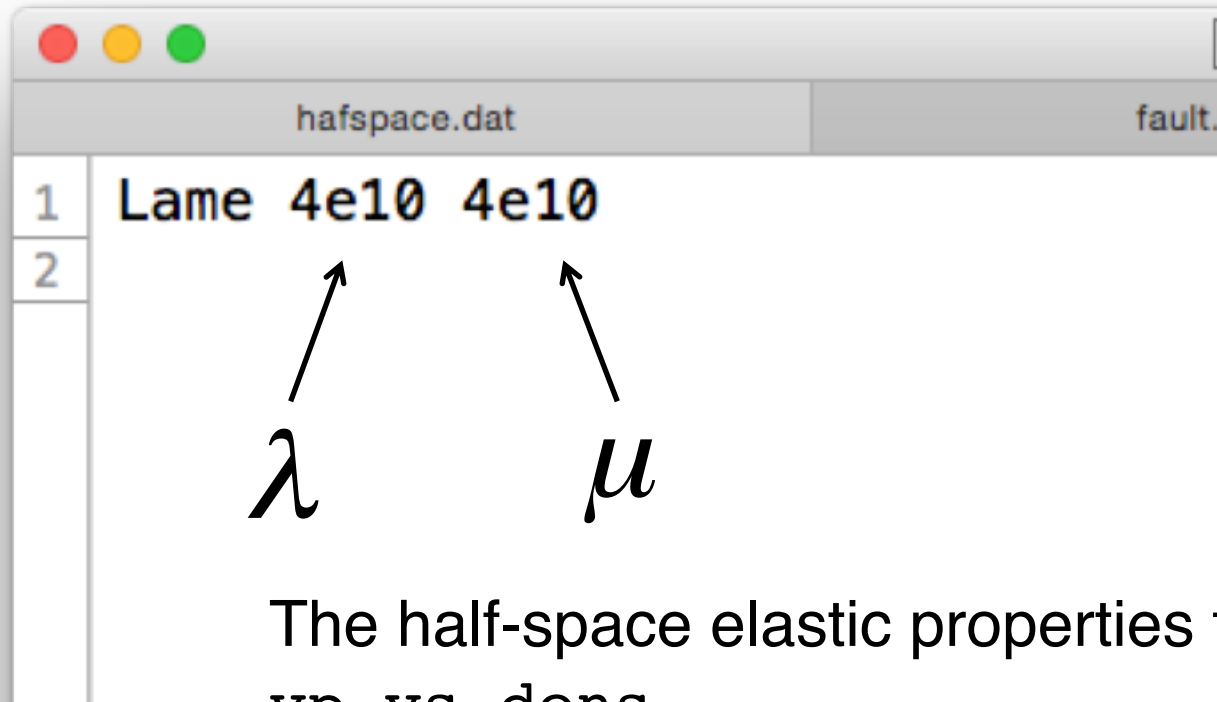
	STLO	STLA	STDP
1	32.1	40.8	15
2	32.2	40.8	15
3	32.3	40.8	15
4	32.0	40.9	15
5	32.0	41.0	15
6	32.0	41.1	15
7			

Activity 1: Strike-Slip Event

- Input files
 - Fault file (fault.dat)
 - Receiver locations (station.dat)
 - Half-space properties (hafspace.dat)

Activity 1: Strike-Slip Event

- hafspace.dat *New file format!*



$$v_p = \sqrt{\frac{\lambda + 2\mu}{\rho}}$$
$$v_s = \sqrt{\frac{\mu}{\rho}}$$
$$\mu = \rho v_s^2$$
$$\lambda = \rho v_p^2 - 2\mu$$

The half-space elastic properties file can be either:
vp vs dens
(as in previous activities), or:
Lame lamda mu
where lamda and mu are the Lamé parameters.

Activity 1: Strike-Slip Event

This input format is similarly deprecated. It also works (for now), but the program will warn you that it is a legacy format and prompt you to use the current format.

***The current format is:
lame 40e9 shear 40e9***

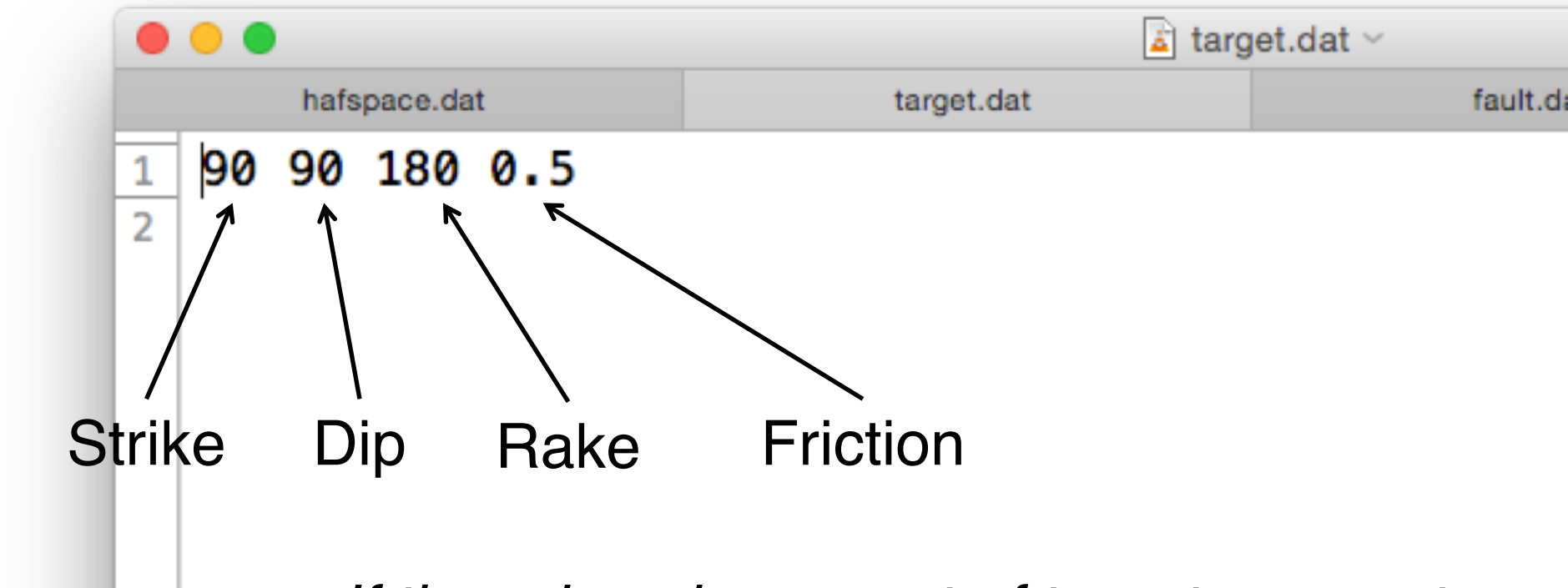
where λ and μ are the Lamé parameters.

Activity 1: Strike-Slip Event

- Input files
 - Fault file (fault.dat)
 - Receiver locations (station.dat)
 - Half-space properties (hafspace.dat)
 - **NEW!** Target fault parameters (target.dat)

Activity 1: Strike-Slip Event

- target.dat



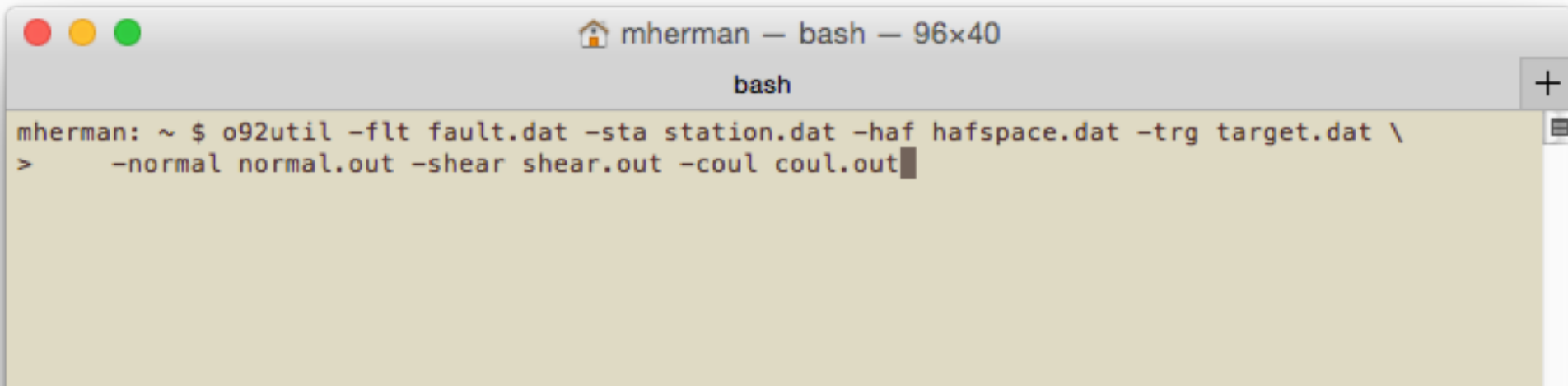
The image shows a screenshot of a text editor window with three tabs: 'hafsace.dat', 'target.dat', and 'fault.d'. The 'target.dat' tab is active and contains a single line of text: '90 90 180 0.5'. Below the text, four arrows point from labels to the respective values: 'Strike' points to '90', 'Dip' points to '90', 'Rake' points to '180', and 'Friction' points to '0.5'. The first column of the table contains the numbers '1' and '2'.

	hafsace.dat	target.dat	fault.d
1		90 90 180 0.5	
2			

If there is only one set of target parameters, then these values are used for every receiver location in station.dat

Activity 1: Strike-Slip Event

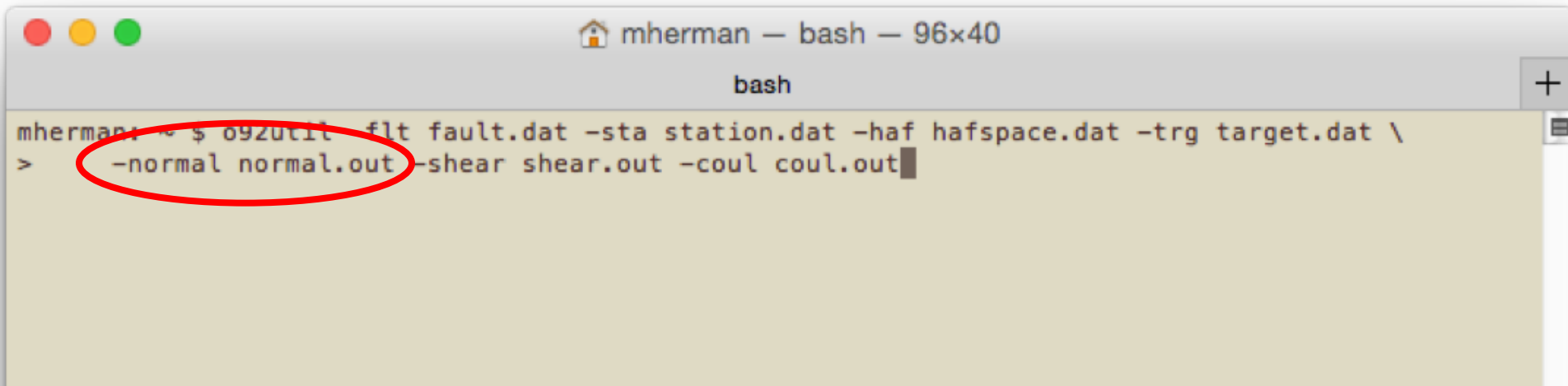
- Output files
 - Normal stress (normal.out)
 - Shear stress (shear.out)
 - Coulomb stress (coul.out)



```
mherman — bash — 96x40
bash
mherman: ~ $ o92util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat \
> -normal normal.out -shear shear.out -coul coul.out
```


Activity 1: Strike-Slip Event

- Output files
 - Normal stress (normal.out)
 - Shear stress (shear.out)
 - Coulomb stress (coul.out)

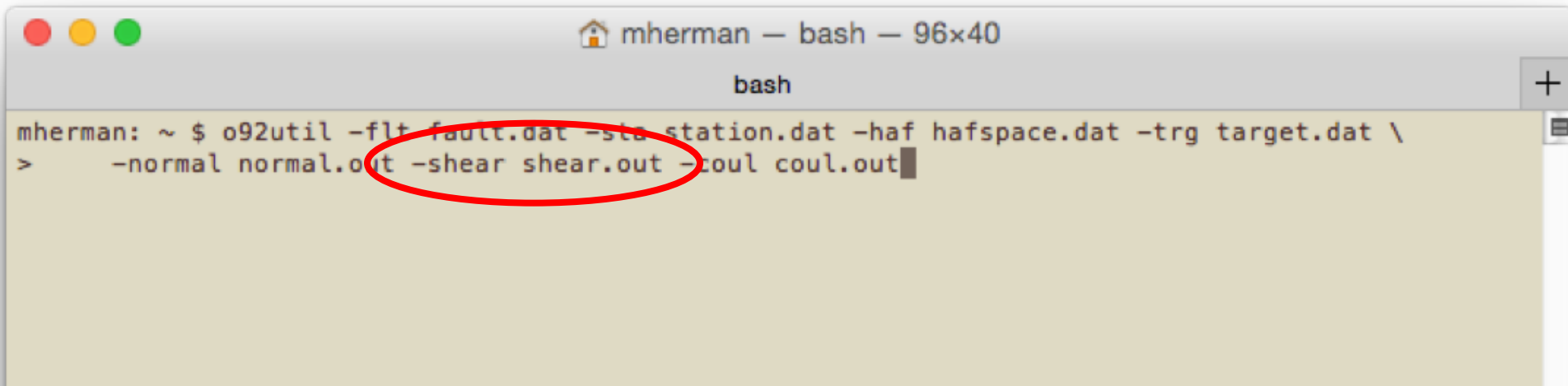


A screenshot of a macOS terminal window titled "mherman — bash — 96x40". The terminal shows a command being entered: `mherman: ~$ 092util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat \`. The next line shows the command being continued: `> -normal normal.out -shear shear.out -coul coul.out`. The text `-normal normal.out` is circled in red. The terminal window has standard macOS window controls (red, yellow, green buttons) and a "+" button in the top right corner.

```
mherman: ~$ 092util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat \  
> -normal normal.out -shear shear.out -coul coul.out
```

Activity 1: Strike-Slip Event

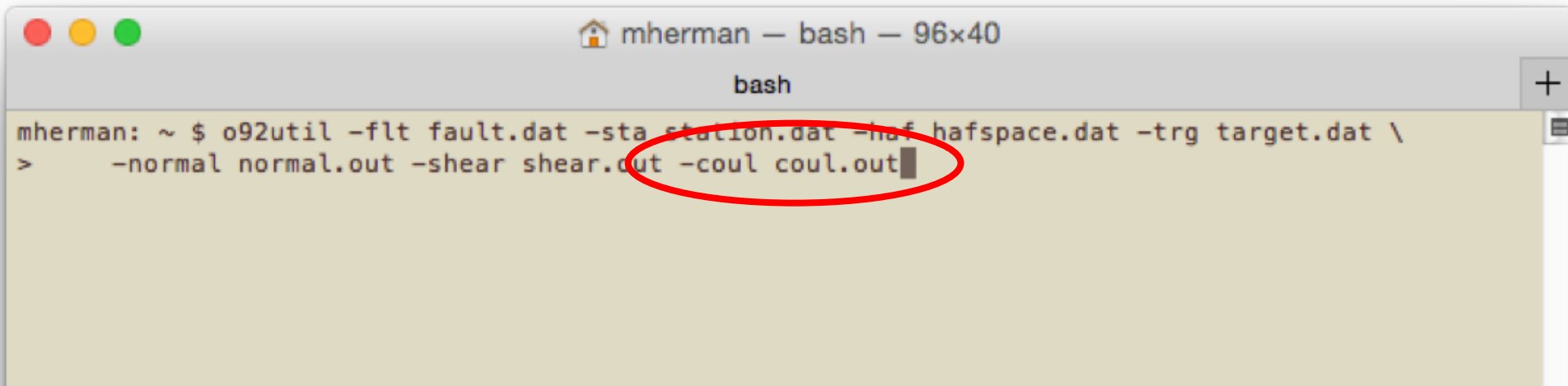
- Output files
 - Normal stress (normal.out)
 - Shear stress (shear.out)
 - Coulomb stress (coul.out)

A screenshot of a macOS terminal window. The title bar shows 'mherman — bash — 96x40'. The terminal content shows a command being entered: 'mherman: ~ \$ o92util -flt faultt.dat -sta station.dat -haf hafspace.dat -trg target.dat \> -normal normal.out -shear shear.out -coul coul.out'. The word 'shear' in the command is circled in red. The terminal window has standard macOS window controls (red, yellow, green buttons) and a '+' button in the top right corner.

```
mherman: ~ $ o92util -flt faultt.dat -sta station.dat -haf hafspace.dat -trg target.dat \  
> -normal normal.out -shear shear.out -coul coul.out
```

Activity 1: Strike-Slip Event

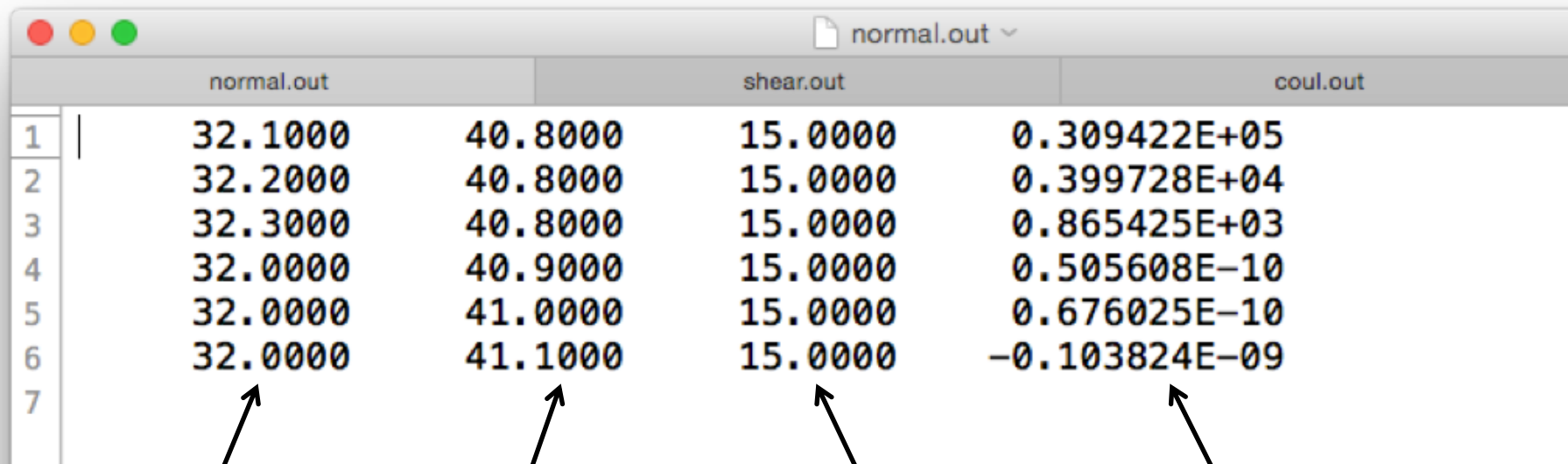
- Output files
 - Normal stress (normal.out)
 - Shear stress (shear.out)
 - Coulomb stress (coul.out)



```
mherman — bash — 96x40
bash
mherman: ~ $ o92util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat \
> -normal normal.out -shear shear.out -coul coul.out
```

Activity 1: Strike-Slip Event

- normal.out



	normal.out		shear.out		coul.out
1	32.1000	40.8000	15.0000		0.309422E+05
2	32.2000	40.8000	15.0000		0.399728E+04
3	32.3000	40.8000	15.0000		0.865425E+03
4	32.0000	40.9000	15.0000		0.505608E-10
5	32.0000	41.0000	15.0000		0.676025E-10
6	32.0000	41.1000	15.0000		-0.103824E-09
7					

STLO

STLA

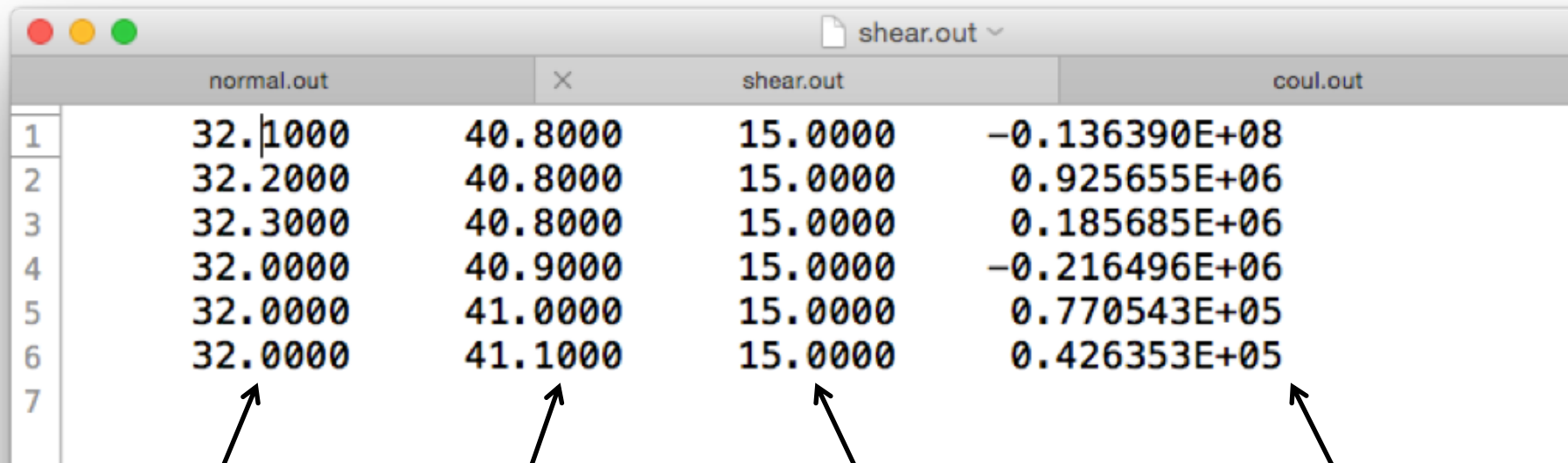
STDP

Normal
Stress
(Pa)

*Negative normal stress implies
compression, positive is dilation.*

Activity 1: Strike-Slip Event

- shear.out



	normal.out		shear.out	coul.out
1	32.1000	40.8000	15.0000	-0.136390E+08
2	32.2000	40.8000	15.0000	0.925655E+06
3	32.3000	40.8000	15.0000	0.185685E+06
4	32.0000	40.9000	15.0000	-0.216496E+06
5	32.0000	41.0000	15.0000	0.770543E+05
6	32.0000	41.1000	15.0000	0.426353E+05
7				

STLO

STLA

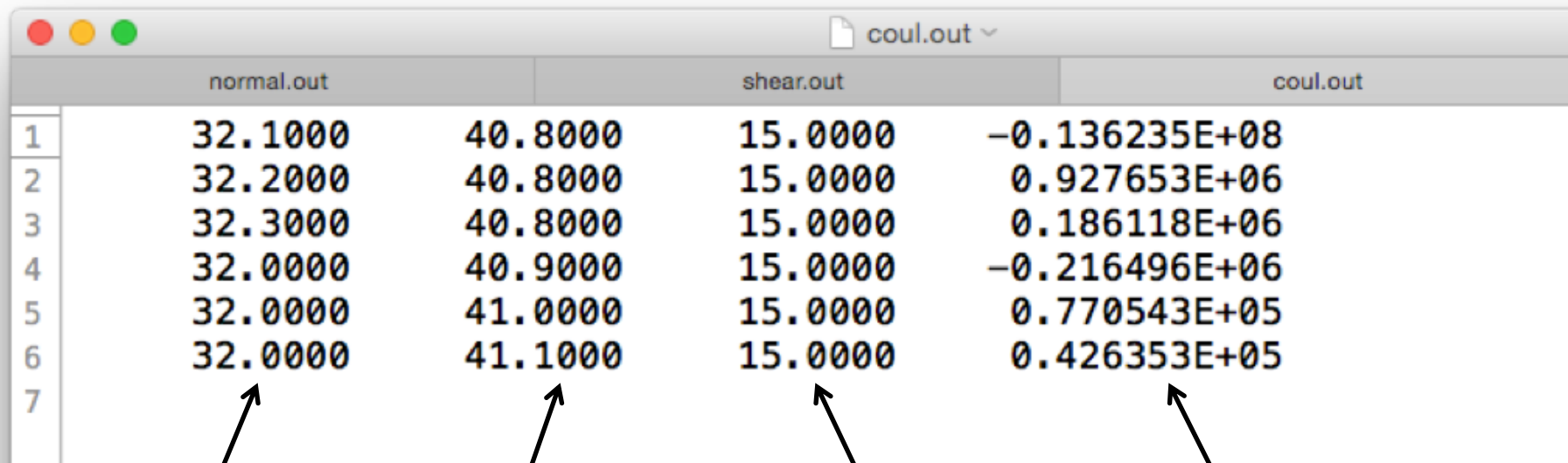
STDP

Shear
Stress
(Pa)

*Shear stress is reported as projected
onto the slip vector. The maximum shear stress is
printed in the 5th column (not shown)*

Activity 1: Strike-Slip Event

- coul.out



A screenshot of a file explorer window titled 'coul.out'. It displays a table with four columns: 'normal.out', 'shear.out', and 'coul.out'. The first column is numbered 1 through 7. The data is as follows:

	normal.out	shear.out	coul.out
1	32.1000	40.8000	15.0000
2	32.2000	40.8000	15.0000
3	32.3000	40.8000	15.0000
4	32.0000	40.9000	15.0000
5	32.0000	41.0000	15.0000
6	32.0000	41.1000	15.0000
7			

STLO

STLA

STDP

Coulomb
Stress
(Pa)

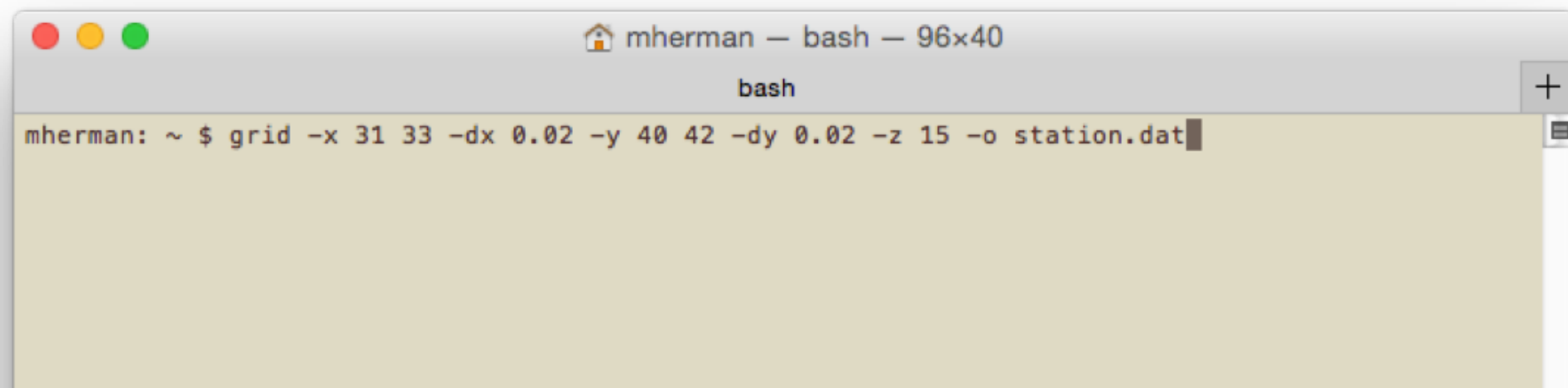
Positive ΔCS : target fault brought closer to failure by the source

Activity 1b: Plotting Stress

- Sometimes it can be insightful to resolve stress at a point (e.g., to determine the stress change on a known fault)
- Other times, it is more useful to plot the stress distribution, as we did this morning
- Start by assuming all target faults have the same kinematics and are at same depth as the source

Activity 1b: Plotting Stress

- Use GRID to create dense set of receivers in station.dat
- Try an increment of 0.02

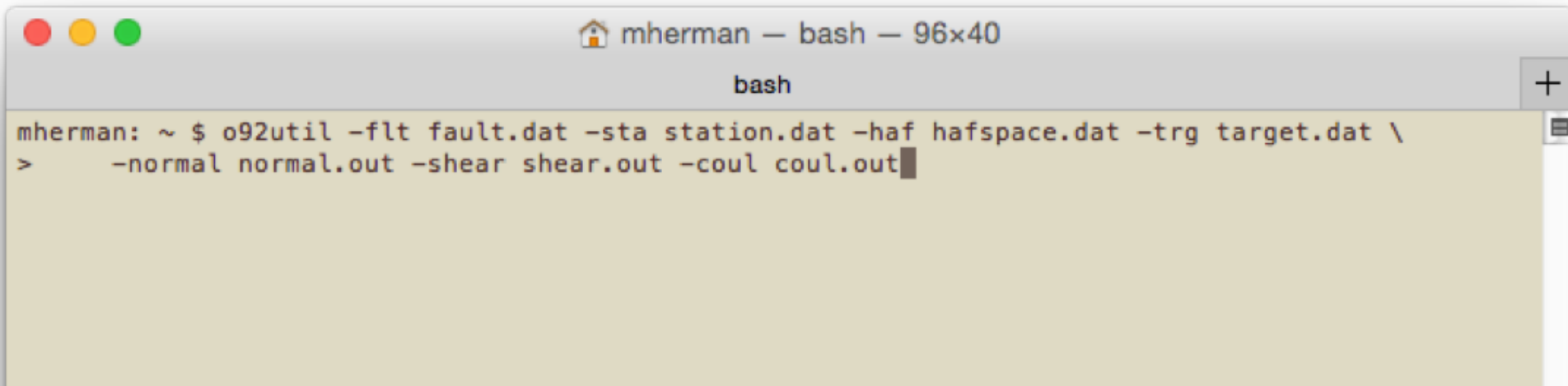


A screenshot of a macOS terminal window. The title bar at the top shows three colored window control buttons (red, yellow, green) on the left, a home icon followed by the text 'mherman — bash — 96x40' in the center, and a plus sign on the right. Below the title bar, the text 'bash' is centered. The main area of the terminal has a light beige background and displays the command 'mherman: ~ \$ grid -x 31 33 -dx 0.02 -y 40 42 -dy 0.02 -z 15 -o station.dat' with a black cursor at the end of the line.

```
mherman: ~ $ grid -x 31 33 -dx 0.02 -y 40 42 -dy 0.02 -z 15 -o station.dat
```


Activity 1b: Plotting Stress

- Run O92UTIL again with same output files
 - Normal stress (normal.out)
 - Shear stress (shear.out)
 - Coulomb stress (coul.out)

A screenshot of a macOS terminal window. The title bar at the top shows three colored window control buttons (red, yellow, green) on the left, a home icon followed by the text 'mherman — bash — 96x40' in the center, and a '+' button on the right. Below the title bar, the word 'bash' is centered. The main area of the terminal is a light beige color and contains the following text: 'mherman: ~ \$ o92util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat \' followed by a new line starting with '>' and '-normal normal.out -shear shear.out -coul coul.out'. The cursor is at the end of the second line.

```
mherman: ~ $ o92util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat \  
> -normal normal.out -shear shear.out -coul coul.out
```

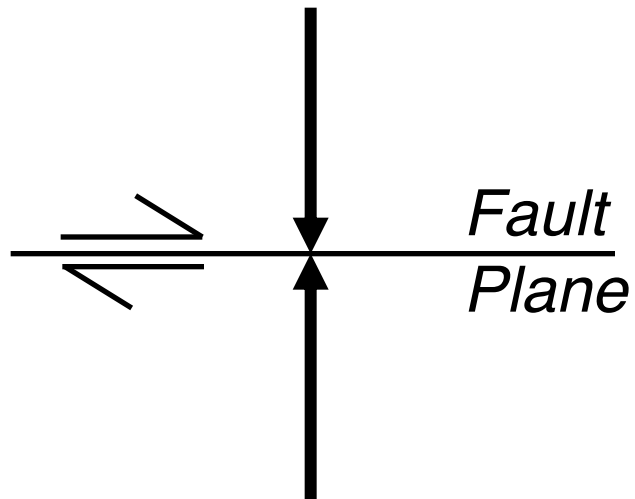
Activity 1b: Plotting Stress

Plot results (basic plotting script provided)

```
plot_stress.sh
1 #!/bin/sh
2
3 #####
4 #      BOURNE SHELL SCRIPT FOR PLOTTING RESOLVED STRESS COMPONENTS
5 #####
6
7 #####
8 #      INPUT/OUTPUT FILES FROM 092UTIL
9 #####
10 # Input source fault file
11 FLT_FILE="fault.dat" # EVLO EVLA EVDP STR DIP RAK SLIP WID LEN
12 # Output normal/shear/Coulomb stress file
13 STS_FILE="normal.out" # STLO STLA STDP STRS
14
15 #####
16 #      GMT PLOTTING VARIABLES
17 #####
18 # Map projection (use 'man psbasemap' to see options)
19 PROJ="-JM4i -P"
20 # Map limits (-RXMIN/XMAX/YMIN/YMAX)
21 LIMS="-R31/33/40/42"
22 # Output PostScript file name
23 PSFILE="stress.ps"
24
25 #####
26 #      GMT PLOTTING COMMANDS
27 #####
28 # Generate color palette for plotting Coulomb stresses
29 makecpt -Cno_green -T-1e5/1e5/1e4 -D > stress.cpt
30
31 # Convert stress output to NetCDF grid file
32 # -Iincr/yincr specifies the grid increments, and should be the same
33 # as the increment used in the grid command
34 awk '{print $1,$2,sqrt($4)}' $STS_FILE |\
35   xyz2grd -Gstress.grd $LIMS -I0.2/0.2
36 # Plot stress grid, using color palette generated above
37 grdimage stress.grd $PROJ $LIMS -Cstress.cpt -K > $PSFILE
38
39 # Draw coastline (-W) and national boundaries (-N1)
40 pscoast $PROJ $LIMS -Dh -W0.75p -N1/0.5p -K -0 >> $PSFILE
41
42 # Plot focal mechanisms of input faults
43 awk '{print $1,$2,$3,$4,$5,$6,$5}' $FLT_FILE |\
44   psmeca $PROJ $LIMS -Sa0.5i -W1p -L1p -Ggrey -K -0 >> $PSFILE
45 # Plot horizontal projection of rectangular input faults
46 # To convert degrees to radians, multiply by pi/180 = 0.01745
47 awk '{print $1,$2,$4,$9,$8*cos($5*0.017)}' $FLT_FILE |\
48   psxy $PROJ $LIMS -SJ -W3p,darkgreen -K -0 >> $PSFILE
49
50 # Draw map outline and label axes
51 psbasemap $PROJ $LIMS -Ba1WeSn -0 >> $PSFILE
```

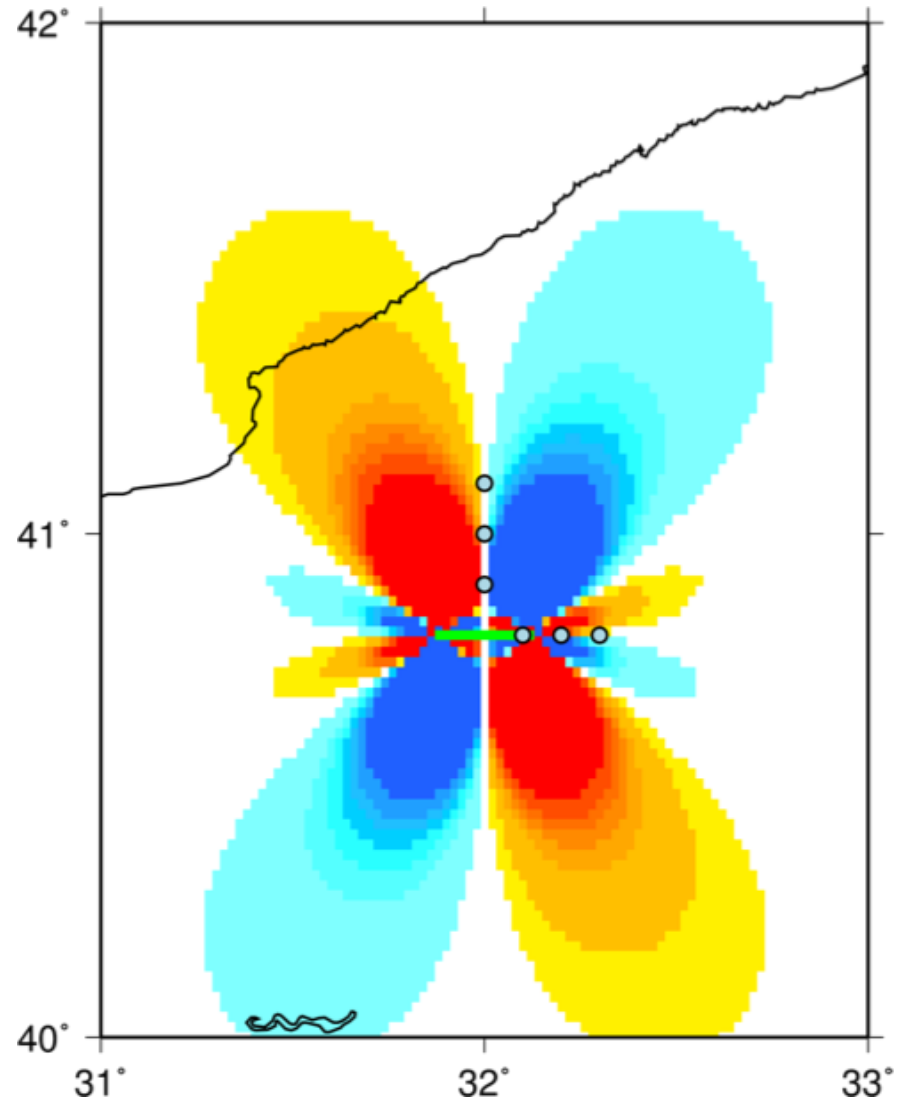
Activity 1b: Plotting Stress

- Normal stress



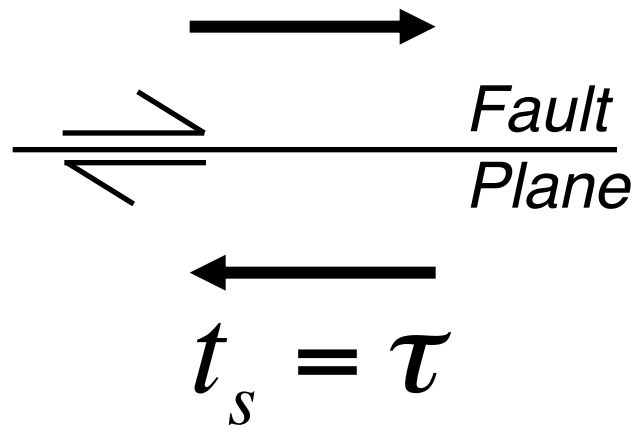
$$t_n = \sigma_n$$

Common notation for normal stress is the Greek letter, sigma.

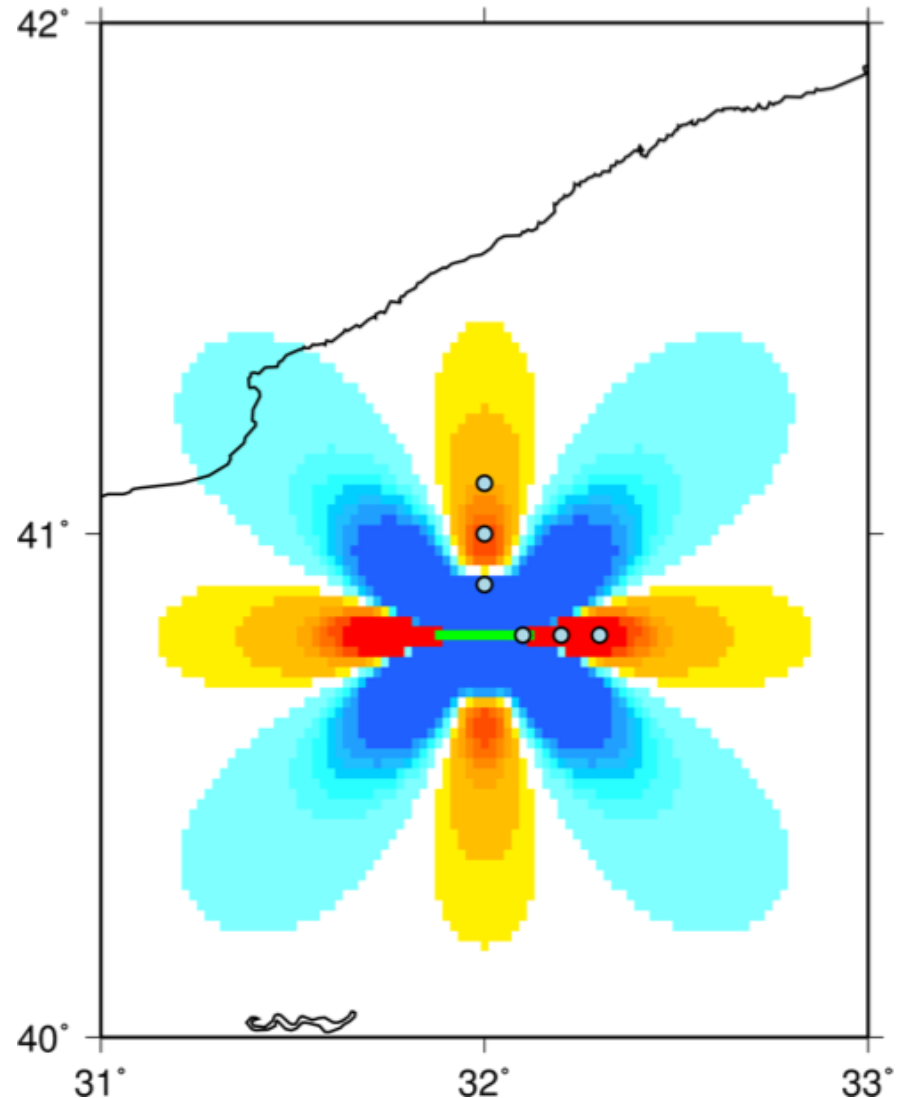


Activity 1b: Plotting Stress

- Shear stress

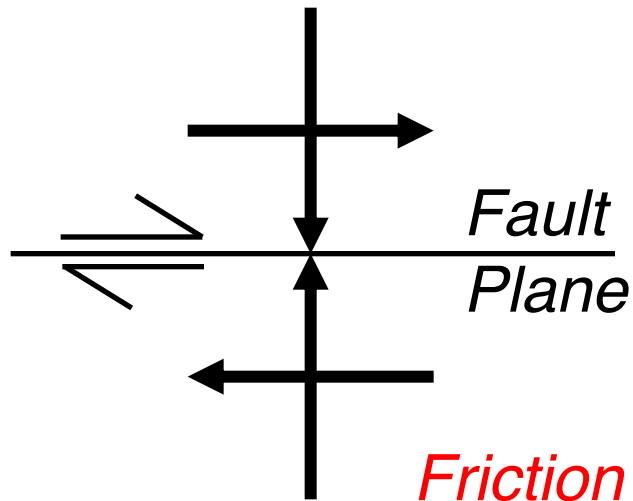


Common notation for shear stress is the Greek letter, tau.



Activity 1b: Plotting Stress

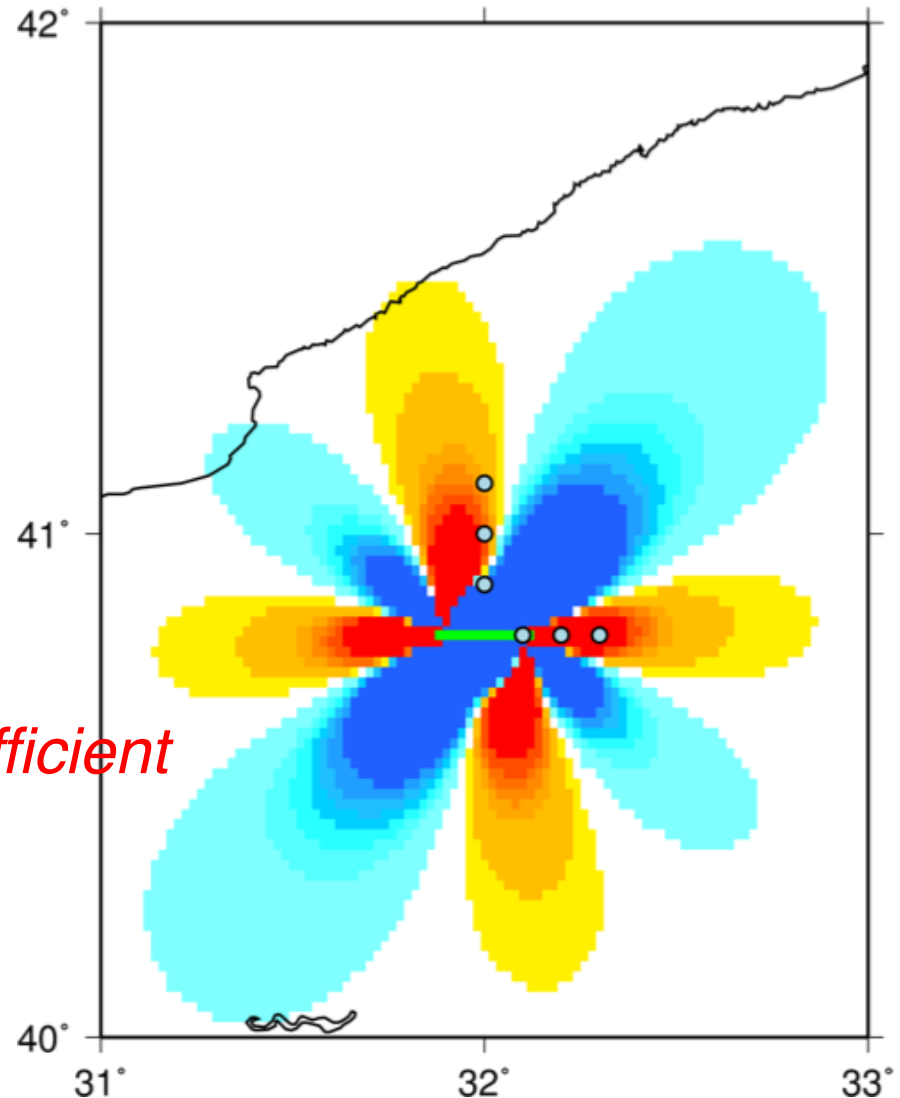
- Coulomb stress



Friction coefficient

$$\Delta CS = t_s - \mu t_n$$

$$\Delta CS = \tau - \mu \sigma_n$$



Activity 2: Thrust EQ Stress

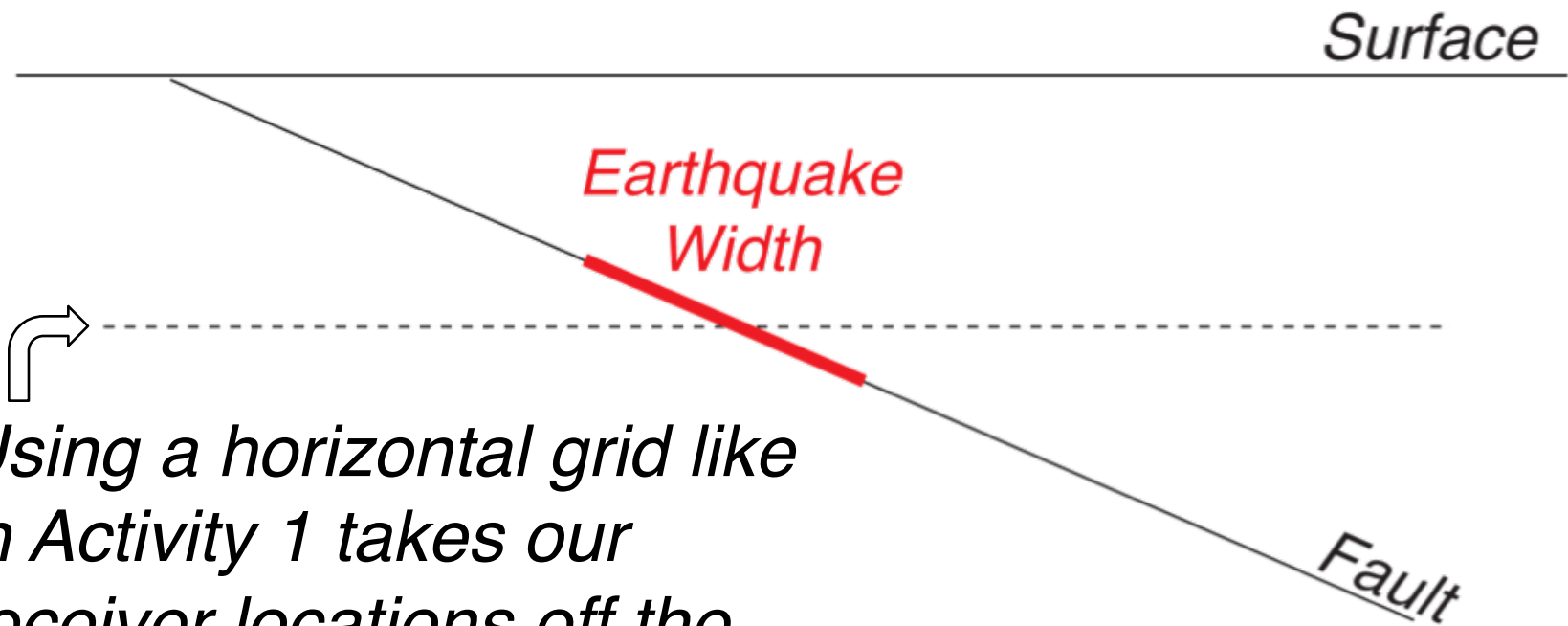
- Most difficult aspect of Δ CS analysis is target fault location and geometry
- This aspect is often ambiguous and occasionally incorrect in literature
- Let us use a thrust faulting earthquake to demonstrate the concept

Activity 2: Thrust EQ Stress

- Thrust faulting earthquakes occur on dipping surfaces (e.g. 2015 Mw 7.8 Nepal, 2014 Mw 8.2 Chile, 2010 Mw 9.0 Tohoku)
- We might think about how stress has changed on the fault around the earthquake

Activity 2: Thrust EQ Stress

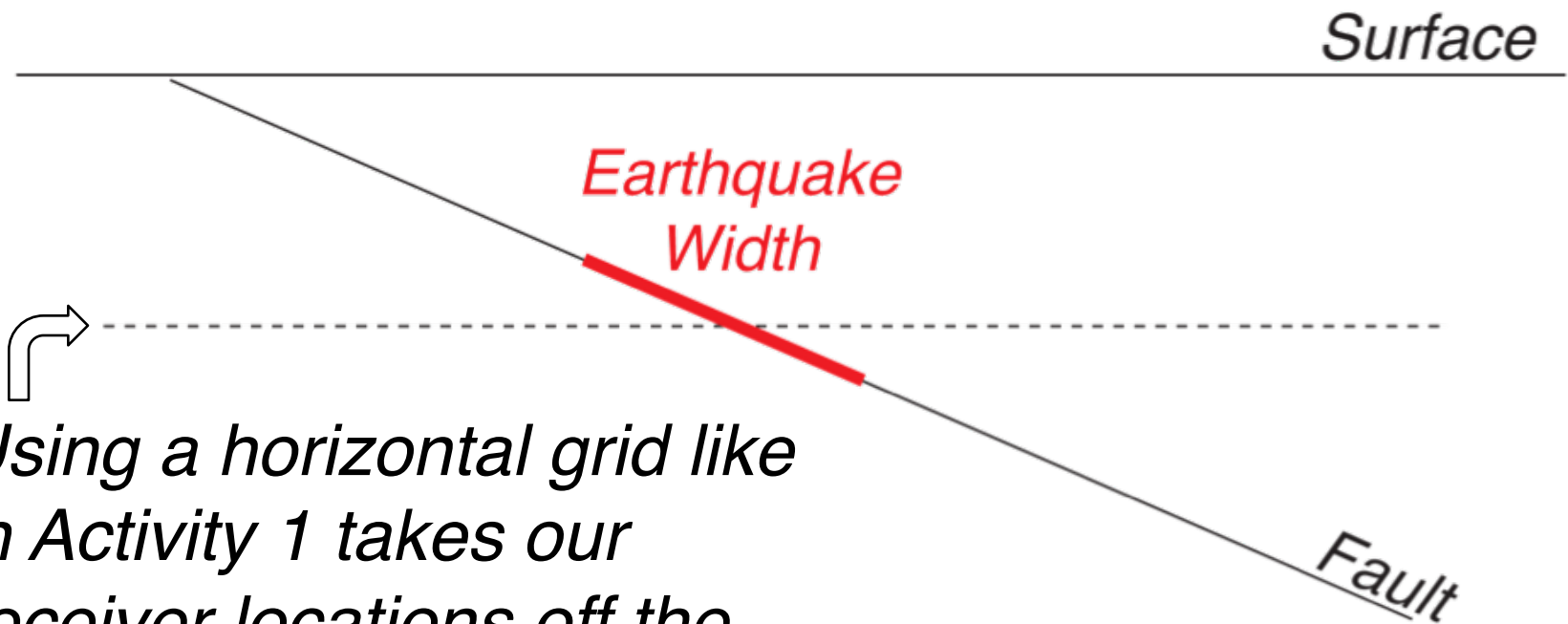
- Cross-section through a thrust fault hosting an earthquake



Using a horizontal grid like in Activity 1 takes our receiver locations off the fault of interest

Activity 2: Thrust EQ Stress

- Cross-section through a thrust fault hosting an earthquake

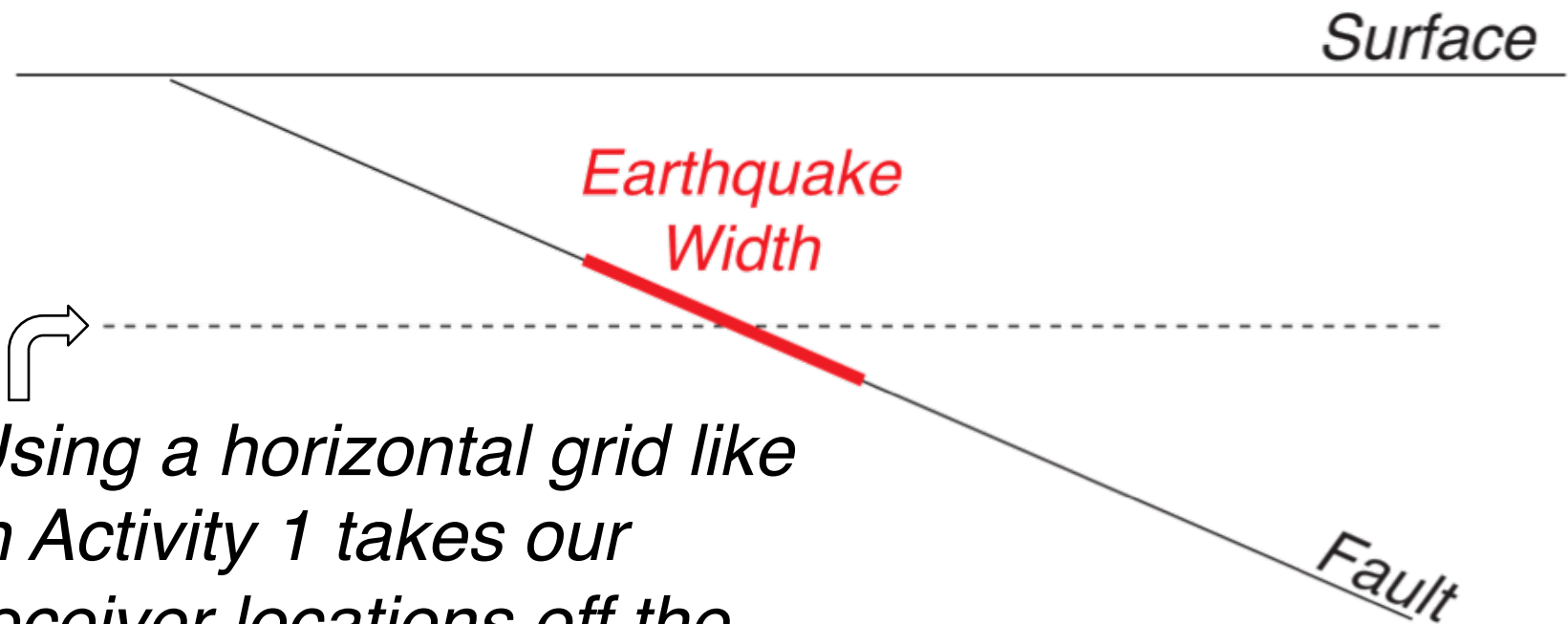


Using a horizontal grid like in Activity 1 takes our receiver locations off the fault of interest

Solution 1: use a grid that lies on the dipping plane.

Activity 2: Thrust EQ Stress

- Cross-section through a thrust fault hosting an earthquake

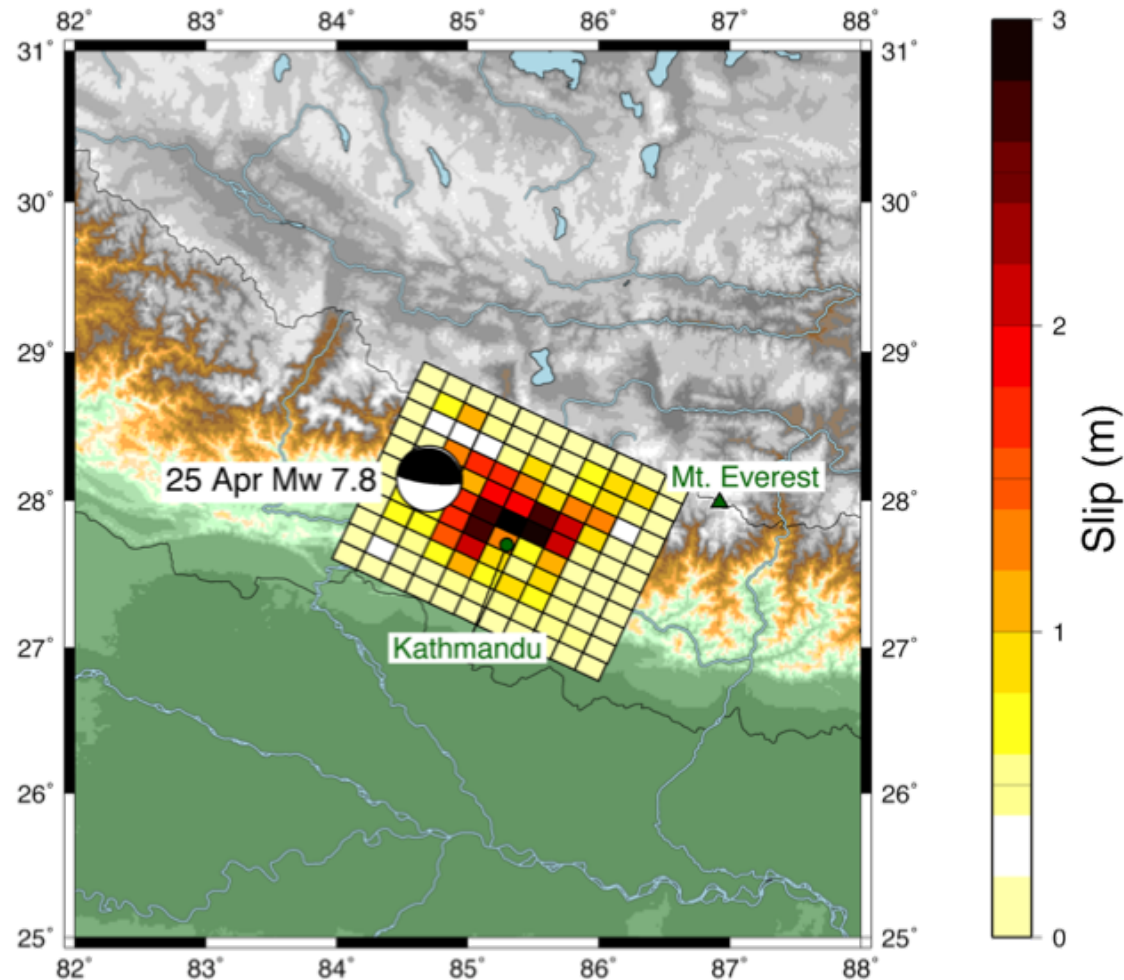


Using a horizontal grid like in Activity 1 takes our receiver locations off the fault of interest

Solution 2: look at the stress in cross-section.

Activity 2: Thrust EQ Stress

- Case study:
2015 Mw 7.8
Nepal
earthquake
- Thrust faulting
event on
shallowly
dipping plane



USGS Finite Fault Model (we will talk about these in more detail soon!)

Activity 2: Thrust EQ Stress

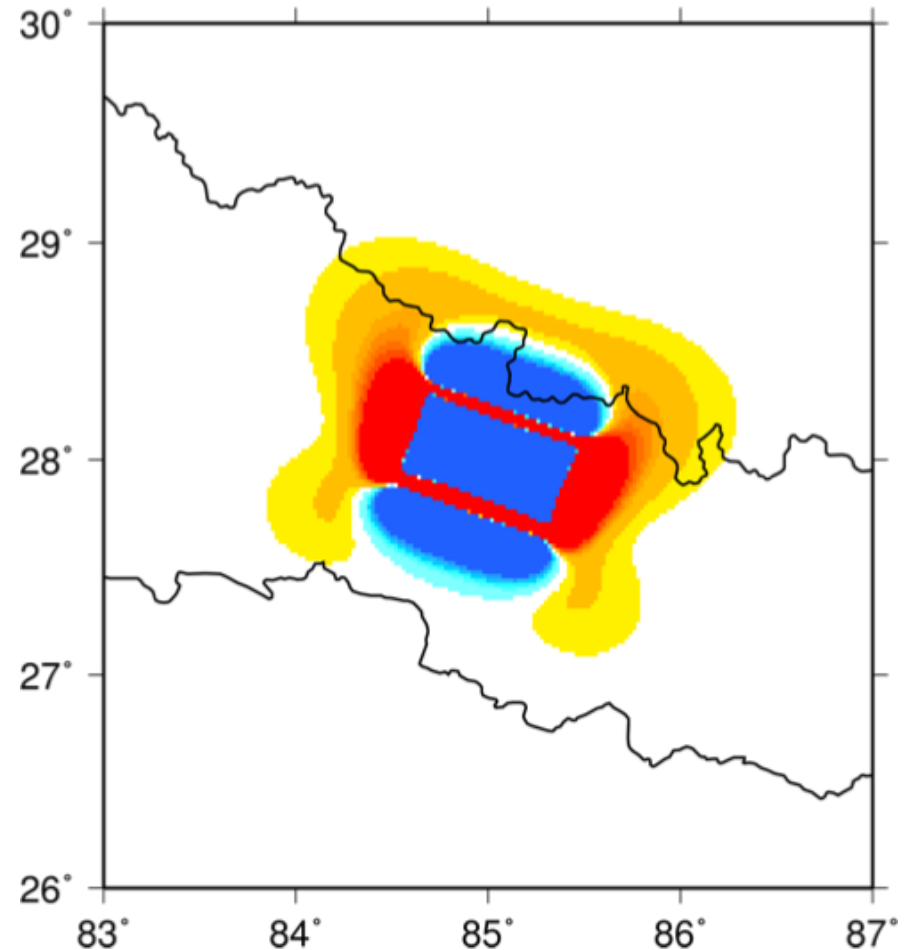
- 2015 Mw 7.8 Nepal earthquake
 - Location: 28°N, 85°E, 15 km
 - Kinematics: strike=-70°, dip=15°, rake=90°
 - Slip: 3.5 m
 - Dimensions: 80 km long, 50 km wide

Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2a: resolve the Coulomb stress change onto a horizontal grid, as in the previous activity*
 - *What should the depth of this grid be?*
 - *Remember to define target fault kinematics!*

Activity 2: Thrust EQ Stress

- Map view of stress on horizontal plane

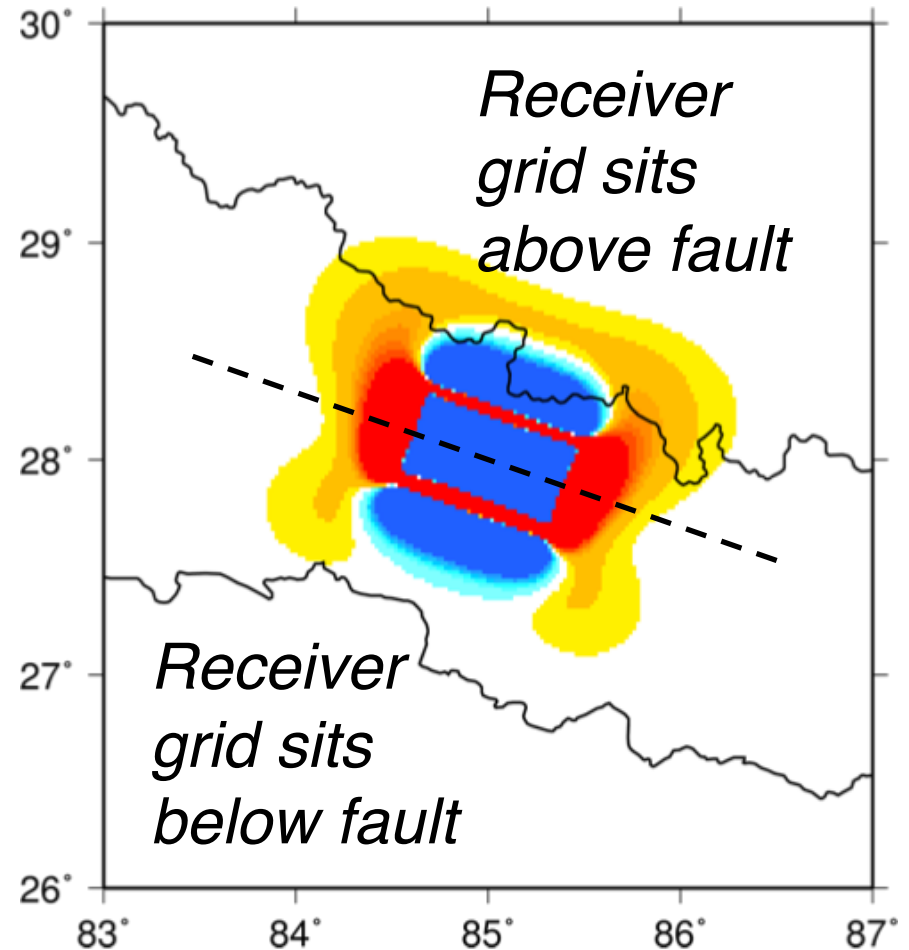
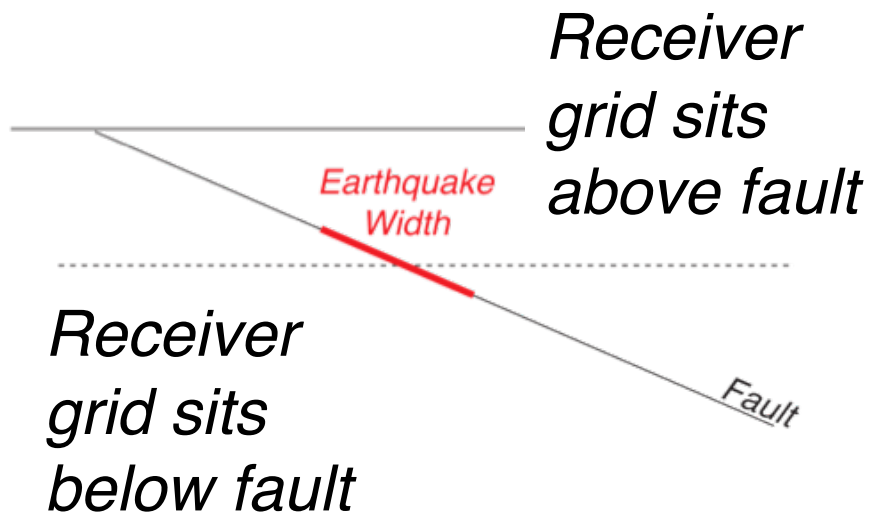


Activity 2: Thrust EQ Stress

```
script.sh
1 #!/bin/sh
2
3 gmtset BASEMAP_TYPE plain
4
5 #####
6 #> INPUT FILES
7 #####
8 # Fault input (Mw 7.8)
9 echo "85 28 15 -70 15 90 3.5 50 80" > fault.dat
10 # Receiver locations
11 D=0.02
12 grid -x 83 87 -dx $D -y 26 30 -dy $D -z 15 -o station.dat
13 # Elastic half-space parameters
14 echo "Lame 35e9 35e9" > hafspace.dat
15 # Target faults
16 echo "-70 15 90 0.5" > target.dat
17
18 #####
19 #> COMPUTE COULOMB STRESS
20 #####
21 o92util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat -coul coul.out
22
23 #####
24 #> PLOT RESULTS
25 #####
26 makecpt -Cno_green -T-1e5/1e5/1e4 -D > coul.cpt
27 PROJ="-JM4i -P"
28 LIMS="-R83/87/26/30"
29 PSFILE="coul.ps"
30 awk '{print $1,$2,$4}' coul.out | \
31     xyz2grd -Gcoul.grd $LIMS -I$D/$D
32 grdimage coul.grd $PROJ $LIMS -Ccoul.cpt -K > $PSFILE
33 pscoast $PROJ $LIMS -N1/1p -Dh -K -O >> $PSFILE
34 psbasemap $PROJ $LIMS -Ba1WeSn -O >> $PSFILE
35
```


Activity 2: Thrust EQ Stress

- Map view of stress on horizontal plane



Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2b: resolve the Coulomb stress change onto the dipping fault*

Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2b: resolve the Coulomb stress change onto the dipping fault*
- Requires computing depth of each point on fault relative to reference point on fault
- GRID is capable of this!

Activity 2: Thrust EQ Stress

Dipping fault using GRID

x-limits and spacing, y-limits and spacing

```
grid -x 83 87 -dx 0.02 -y 26 30 -dy 0.02
```

Geographical parameters are defined the same way as for horizontal grid.

Activity 2: Thrust EQ Stress

Dipping fault using GRID

x-limits and spacing, y-limits and spacing,
reference point and geometry, output file

```
grid -x 83 87 -dx 0.02 -y 26 30 -dy 0.02  
-dip 85 28 15 -70 15 -geo -o station.dat
```

Longitude Latitude Depth
 (km)



*Location of reference
point on plane*

Activity 2: Thrust EQ Stress

Dipping fault using GRID

x-limits and spacing, y-limits and spacing,
reference point and geometry, output file

```
grid -x 83 87 -dx 0.02 -y 26 30 -dy 0.02  
    -dip 85 28 15 -70 15 -geo -o station.dat
```

Strike

Dip

Orientation of plane

Activity 2: Thrust EQ Stress

Dipping fault using GRID

x-limits and spacing, y-limits and spacing,
reference point and geometry, output file

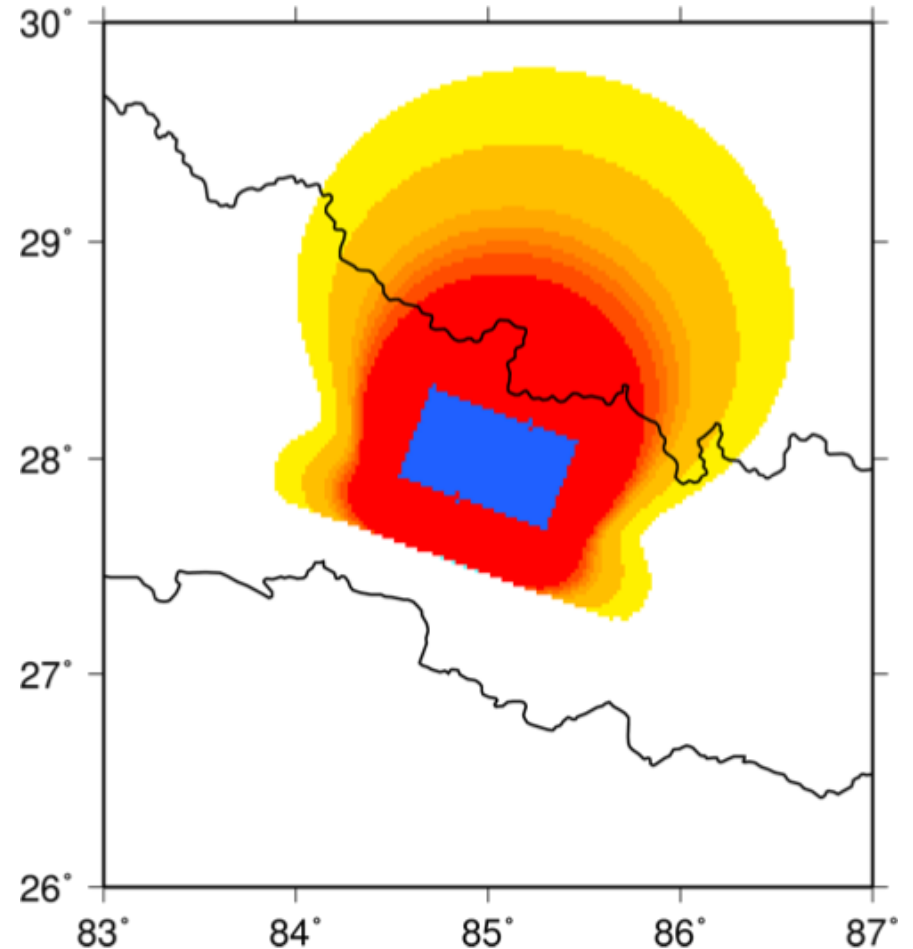
```
grid -x 83 87 -dx 0.02 -y 26 30 -dy 0.02  
    -dip 85 28 15 -70 15 -geo -o station.dat
```

The origin definition is in
geographic coordinates

Orientation of plane

Activity 2: Thrust EQ Stress

- Map view of stress on dipping plane

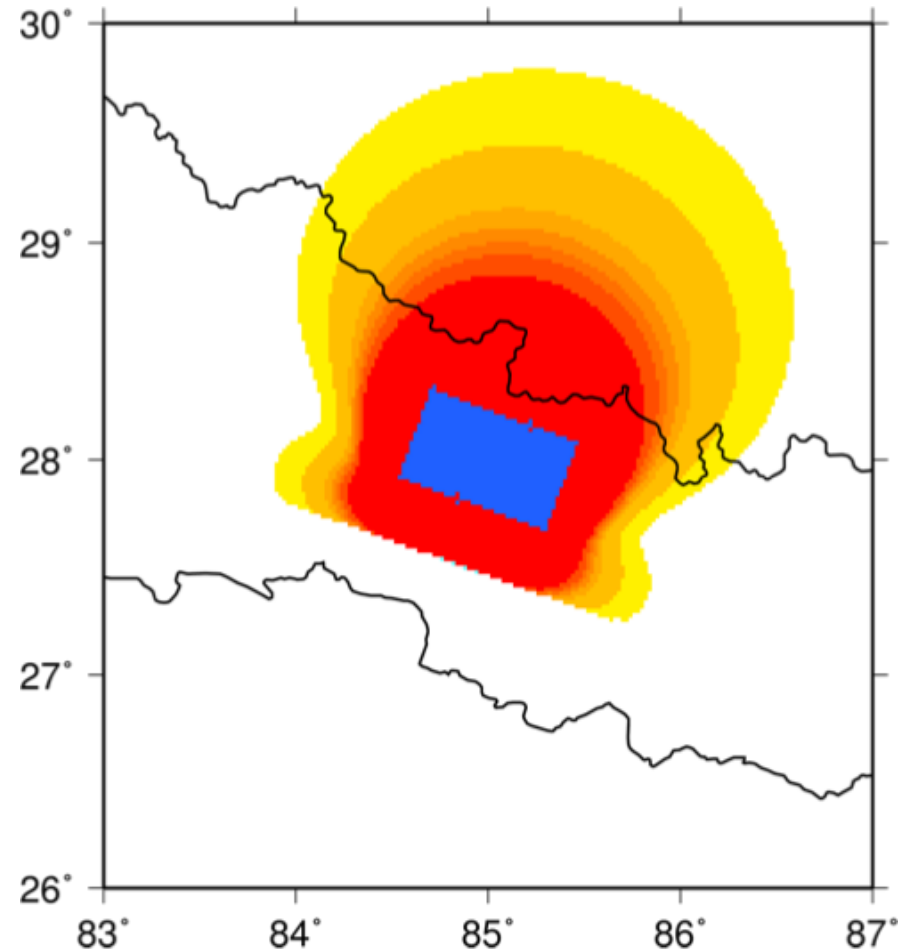


Activity 2: Thrust EQ Stress

```
script.sh
1 #!/bin/sh
2
3 gmtset BASEMAP_TYPE plain
4
5 #####
6 #> INPUT FILES
7 #####
8 # Fault input (Mw 7.8)
9 echo "85 28 15 -70 15 90 3.5 50 80" > fault.dat
10 # Receiver locations
11 D=0.02
12 grid -x 83 87 -dx $D -y 26 30 -dy $D -dip 85 28 15 -70 15 -o station.dat Add -geo!
13 # Elastic half-space parameters
14 echo "Lame 35e9 35e9" > hafspace.dat
15 # Target faults
16 echo "-70 15 90 0.5" > target.dat
17
18 #####
19 #> COMPUTE COULOMB STRESS
20 #####
21 o92util -flt fault.dat -sta station.dat -haf hafspace.dat -trg target.dat -coul coul.out
22
23 #####
24 #> PLOT RESULTS
25 #####
26 makecpt -Cno_green -T-1e5/1e5/1e4 -D > coul.cpt
27 PROJ="-JM4i -P"
28 LIMS="-R83/87/26/30"
29 PSFILE="coul.ps"
30 awk '{print $1,$2,$4}' coul.out | \
31     xyz2grd -Gcoul.grd $LIMS -I$D/$D
32 grdimage coul.grd $PROJ $LIMS -Ccoul.cpt -K > $PSFILE
33 pscoast $PROJ $LIMS -N1/1p -Dh -K -O >> $PSFILE
34 psbasemap $PROJ $LIMS -Ba1WeSn -O >> $PSFILE
35
```

Activity 2: Thrust EQ Stress

- Map view of stress on dipping plane
- More consistent with our intuition:
 - ΔCS lowered in rupture zone
 - Up- and down-dip are loaded
 - Minor effect along-strike



Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2c: resolve the Coulomb stress change in cross-section*

Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2c: resolve the Coulomb stress change in cross-section*
- Now we need a very different grid from the map views we have been using.
- Again, GRID can do this!

Activity 2: Thrust EQ Stress

Vertical cross-section using GRID

x-limits and spacing, z-limits and spacing

grid -x -100 100 -dx 1 -z 0 100 -dz 1

Along-section minimum (km)	Along-section maximum (km)	Minimum Depth (km)	Maximum Depth (km)
----------------------------------	----------------------------------	--------------------------	--------------------------

Activity 2: Thrust EQ Stress

Vertical cross-section using GRID

x-limits and spacing, z-limits and spacing,
reference point and orientation, output file

```
grid -x -100 100 -dx 1 -z 0 100 -dz 1  
-xsec 85 28 20 -geo -o station.dat
```

Longitude Latitude Strike

*Location of origin of
cross-section, and
strike of section*

Activity 2: Thrust EQ Stress

Vertical cross-section using GRID

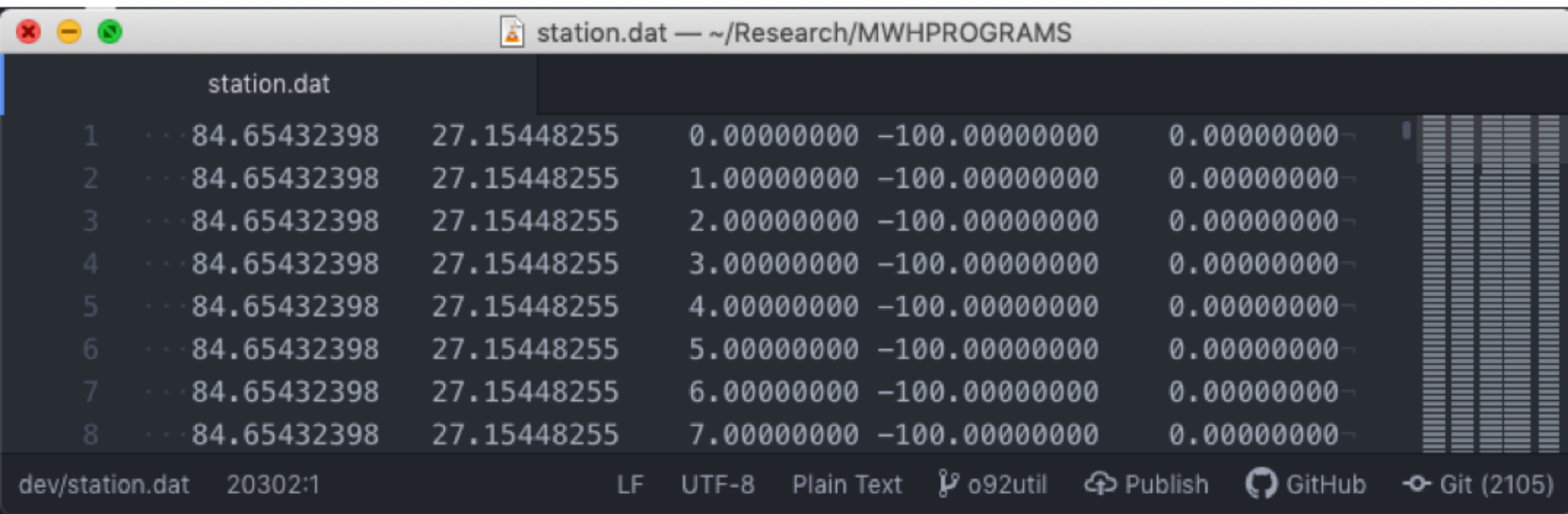
x-limits and spacing, y-limits and spacing,
reference point and orientation, output file

```
grid -x -100 100 -dx 1 -z 0 100 -dz 1  
-xsec 85 28 20 -geo -o station.dat
```

This produces a file with longitude, latitude and depth (for use with O92UTIL), plus two extra columns for the distance along the cross-section (x) and the perpendicular distance (y).

Activity 2: Thrust EQ Stress

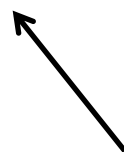
Receiver file (station.dat)

A screenshot of a code editor window titled 'station.dat' with a path of '~ / Research / MWHPROGRAMS'. The editor displays a table with 8 rows of data. The first two columns are constant values: 84.65432398 and 27.15448255. The next three columns show a linear progression from 0.00000000 to 7.00000000, -100.00000000, and 0.00000000 respectively. The bottom status bar shows 'dev/station.dat', '20302:1', and various icons for file encoding (LF, UTF-8), text format (Plain Text), and version control (Git, GitHub).

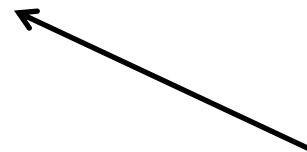
	station.dat				
1	84.65432398	27.15448255	0.00000000	-100.00000000	0.00000000
2	84.65432398	27.15448255	1.00000000	-100.00000000	0.00000000
3	84.65432398	27.15448255	2.00000000	-100.00000000	0.00000000
4	84.65432398	27.15448255	3.00000000	-100.00000000	0.00000000
5	84.65432398	27.15448255	4.00000000	-100.00000000	0.00000000
6	84.65432398	27.15448255	5.00000000	-100.00000000	0.00000000
7	84.65432398	27.15448255	6.00000000	-100.00000000	0.00000000
8	84.65432398	27.15448255	7.00000000	-100.00000000	0.00000000



Longitude



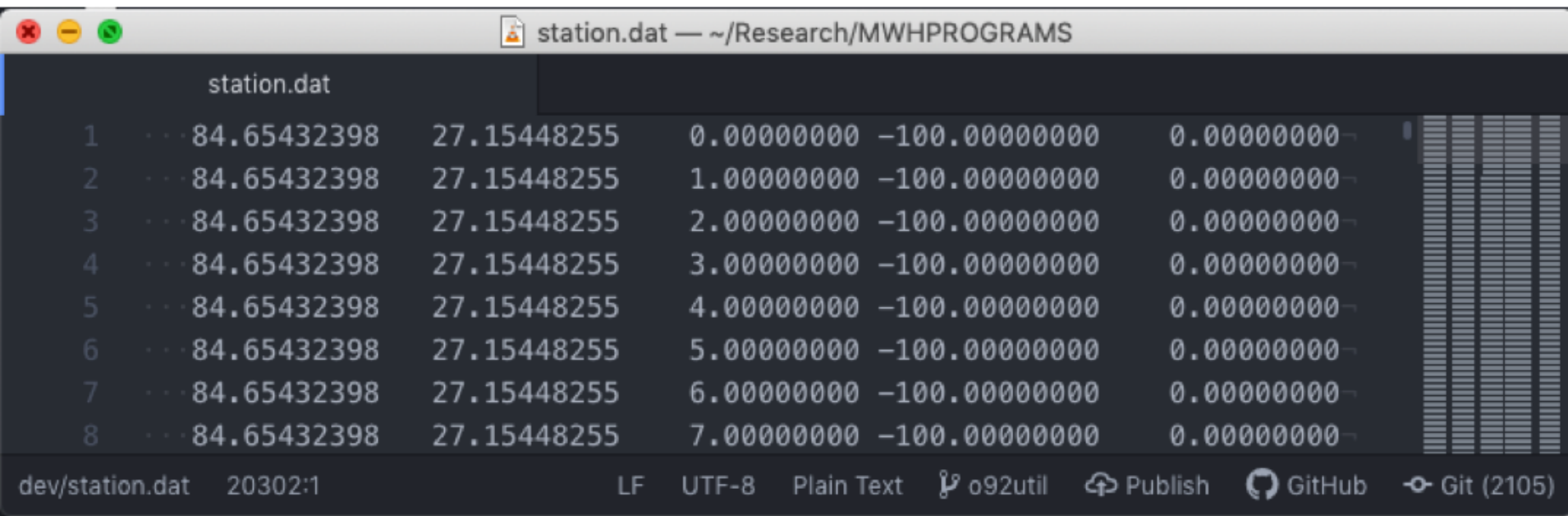
Latitude



Depth

Activity 2: Thrust EQ Stress

Receiver file (station.dat)



station.dat				
1	84.65432398	27.15448255	0.00000000	-100.00000000
2	84.65432398	27.15448255	1.00000000	-100.00000000
3	84.65432398	27.15448255	2.00000000	-100.00000000
4	84.65432398	27.15448255	3.00000000	-100.00000000
5	84.65432398	27.15448255	4.00000000	-100.00000000
6	84.65432398	27.15448255	5.00000000	-100.00000000
7	84.65432398	27.15448255	6.00000000	-100.00000000
8	84.65432398	27.15448255	7.00000000	-100.00000000

dev/station.dat 20302:1 LF UTF-8 Plain Text o92util Publish GitHub Git (2105)

To plot the cross-section, we will also want a file with X-Z values.

Distance along
cross-section

Perp. distance
to cross-section

Activity 2: Thrust EQ Stress

Plot results (basic plotting script provided)

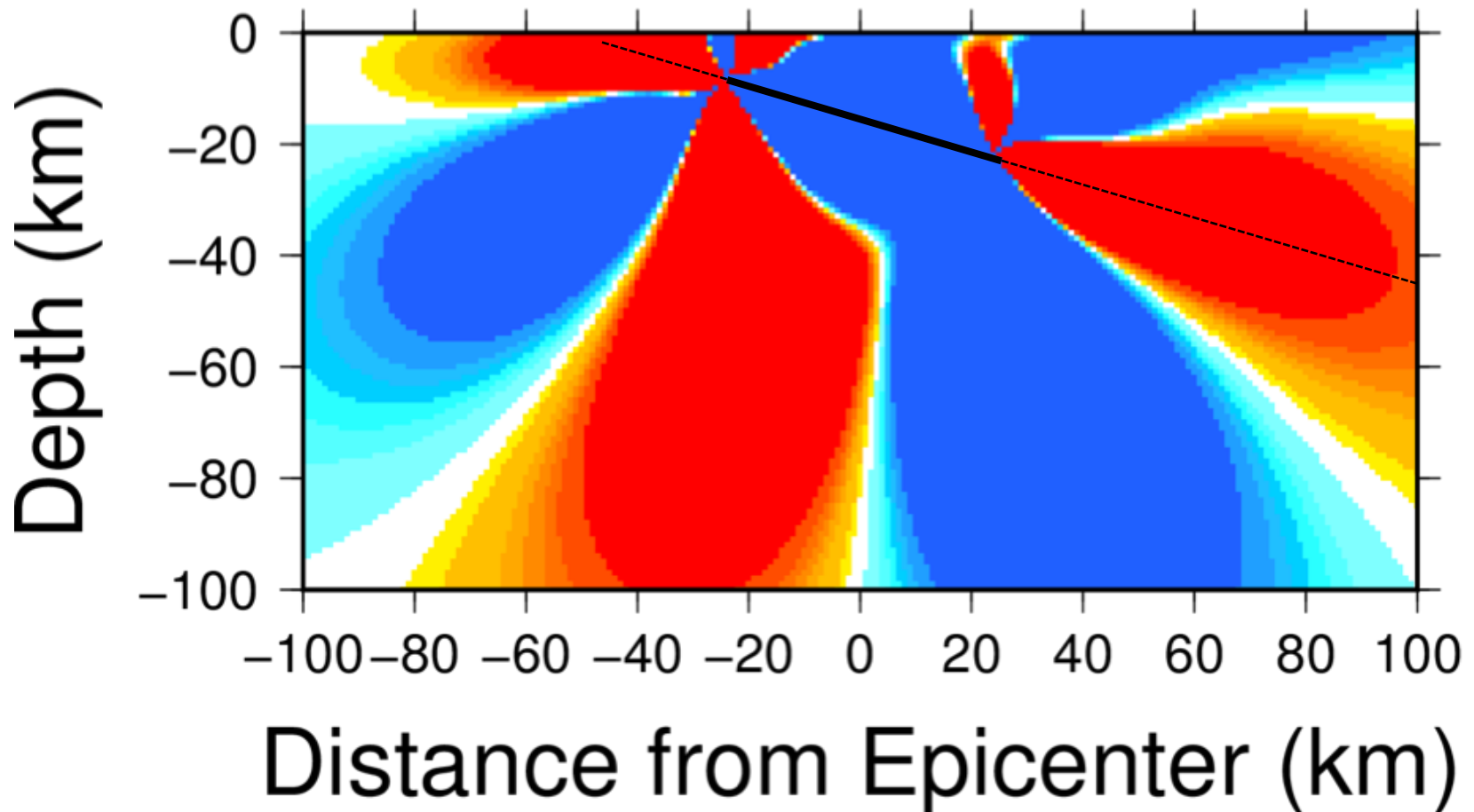
plot_xsec.sh

plot_xsec.sh

```
1  #!/bin/sh
2
3  makecpt -Cno_green -T-1e5/1e5/1e4 -D > stress.cpt
4
5  PROJ="-Jx0.02i -P"
6  LIMS="-R-100/100/-100/0"
7  PSFILE="xsec.ps"
8
9  # Paste is a UNIX tool that appends two text files.
10 # These two files correspond line by line, so we use paste,
11 # then extract the x-distance, depth and CS with awk.
12 paste coul.out xsec.dat | \
13 awk '{print $5, $6, $4}' | \
14 xyz2grd -Gcoul.grd $LIMS -I0.02/0.02 -I1/1
15 grdimage coul.grd $PROJ $LIMS -Ccoul.cpt -K > $PSFILE
16 psbasemap $PROJ $LIMS -Ba20WeSn -O >> $PSFILE
17
```

Activity 2: Thrust EQ Stress

- Cross-section of Coulomb stress

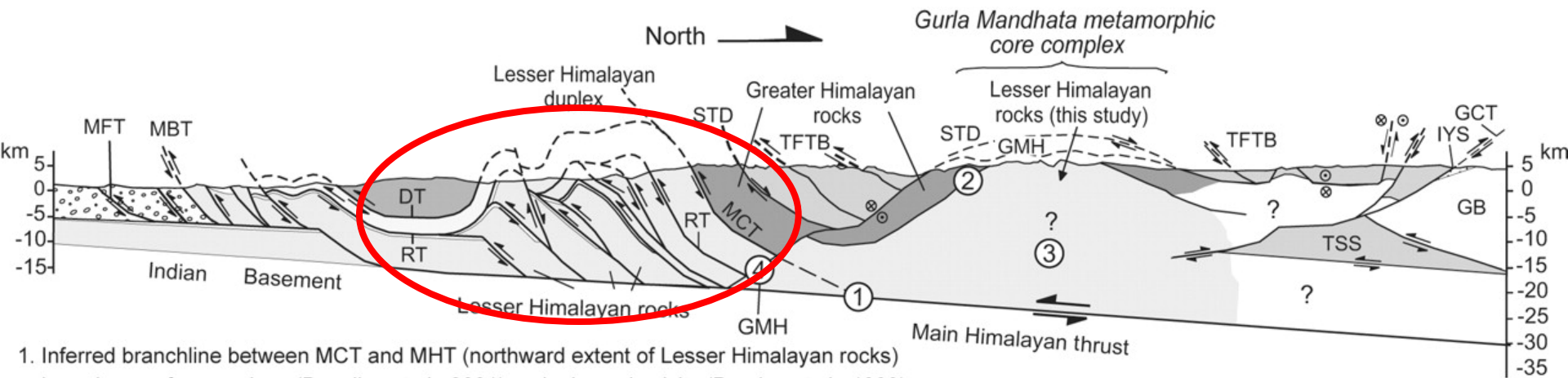


Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2d: resolve the Coulomb stress change on faults dipping 35° in cross-section*
 - *The faults in the upper plate of the collision zone likely dip more steeply than the main plate boundary detachment*

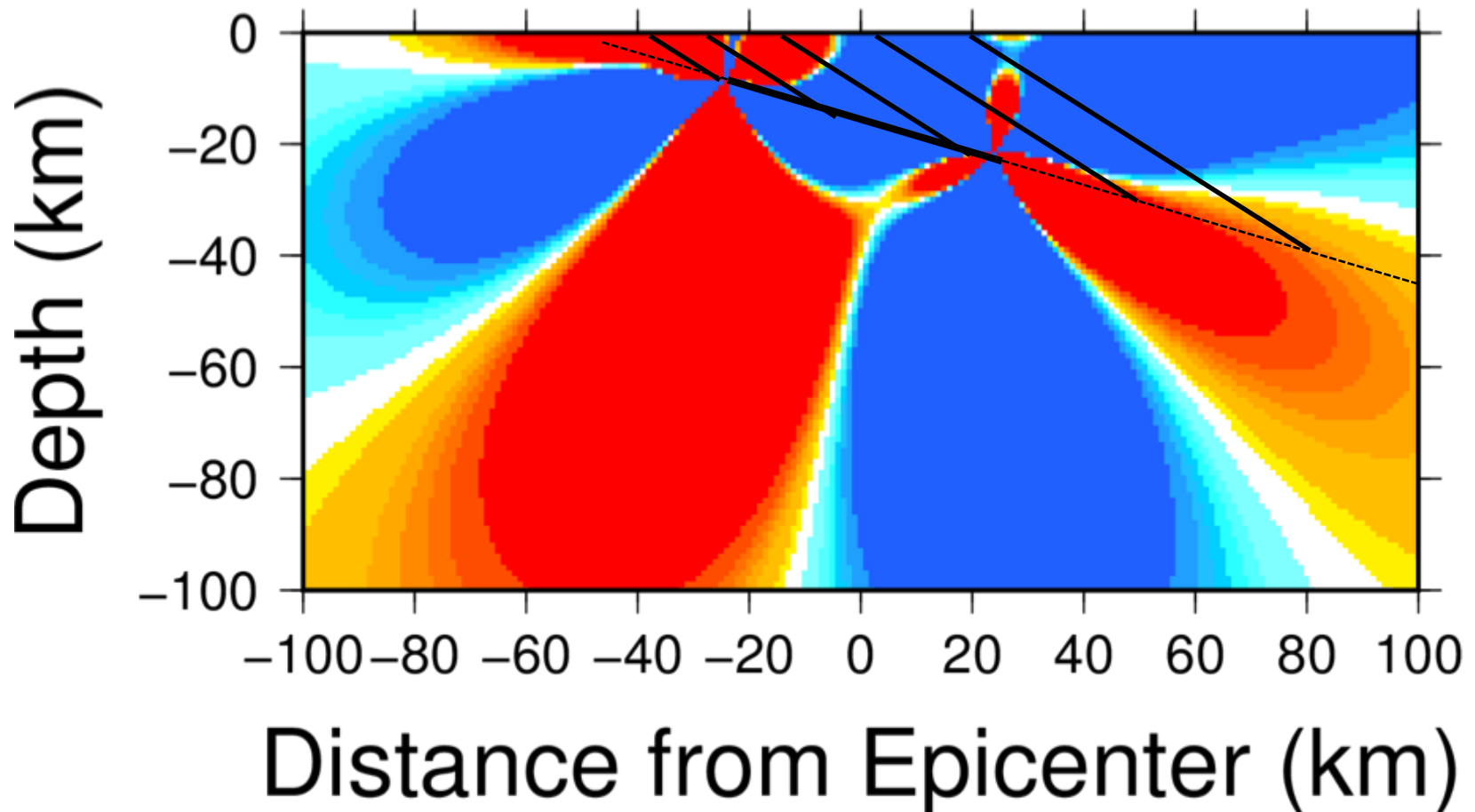
Activity 2: Thrust EQ Stress

- 2015 Mw 7.8 Nepal earthquake
- *Exercise 2d: resolve the Coulomb stress change on faults dipping 35° in cross-section*



Activity 2: Thrust EQ Stress

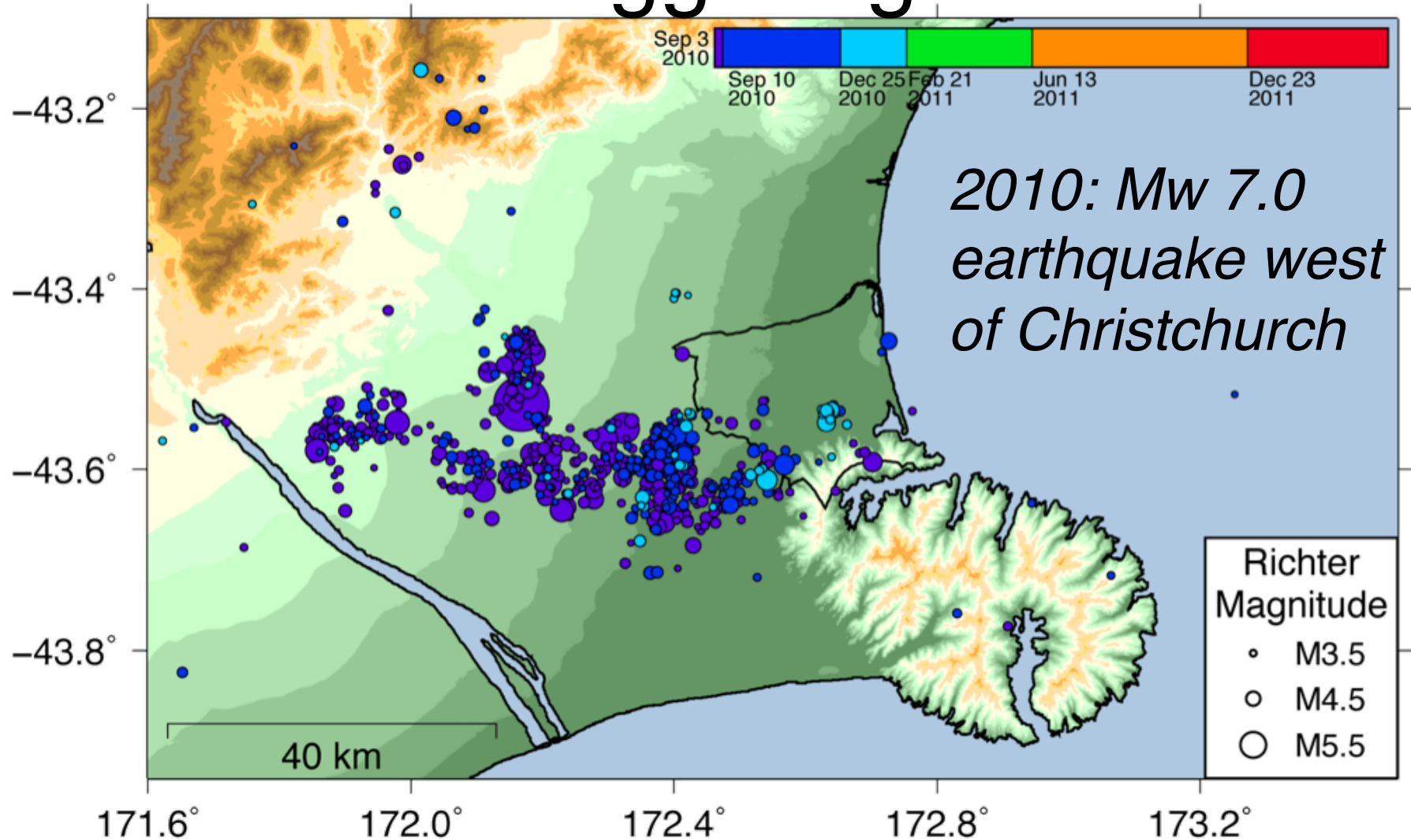
- Cross-section of Coulomb stress



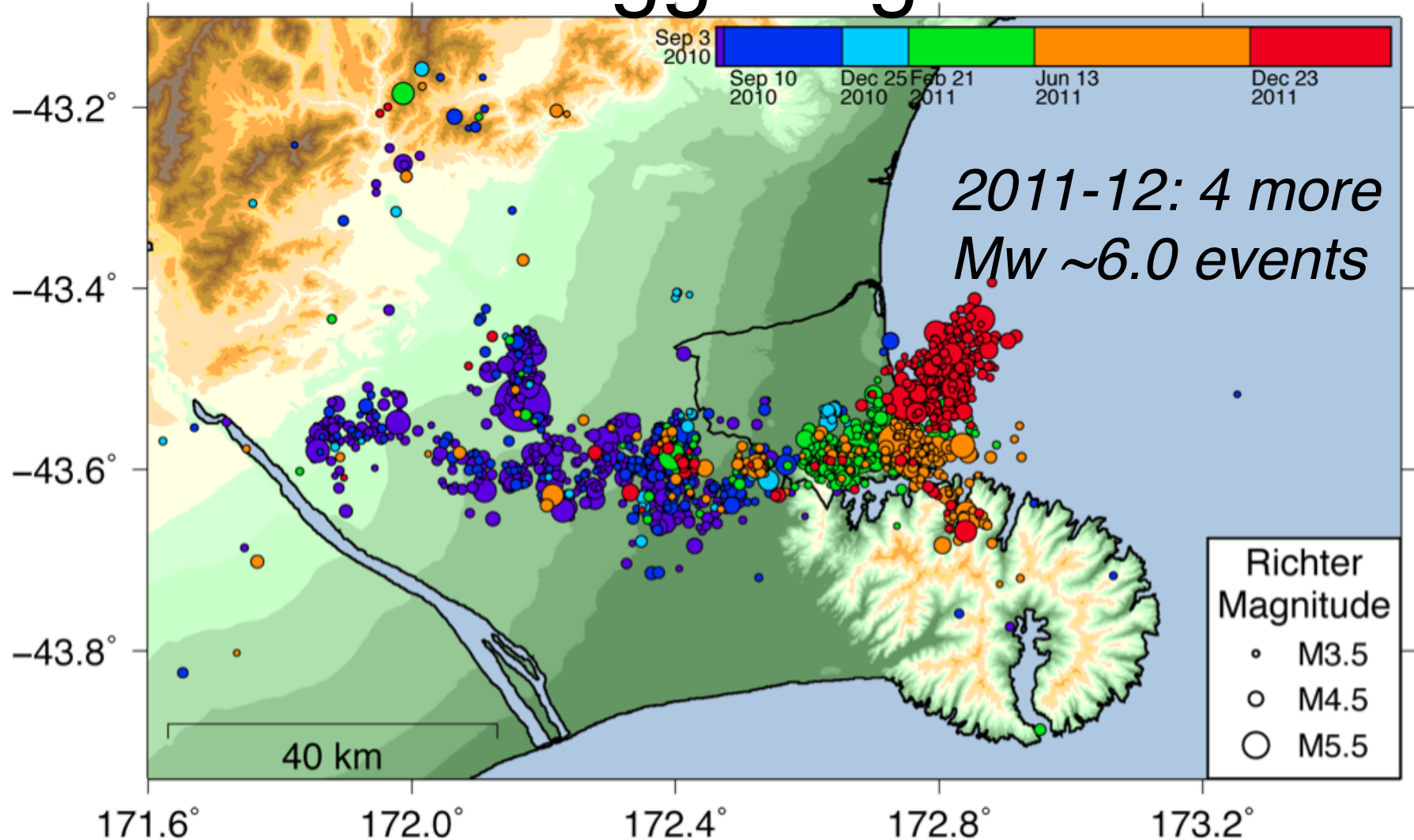
Activity 3: Earthquake Triggering

- Observation: earthquakes commonly occur near previous events
- Does the previous event trigger the subsequent earthquake?
- Correlation in space and time not sufficient to conclude triggering
- ΔCS is a mechanism for earthquake triggering

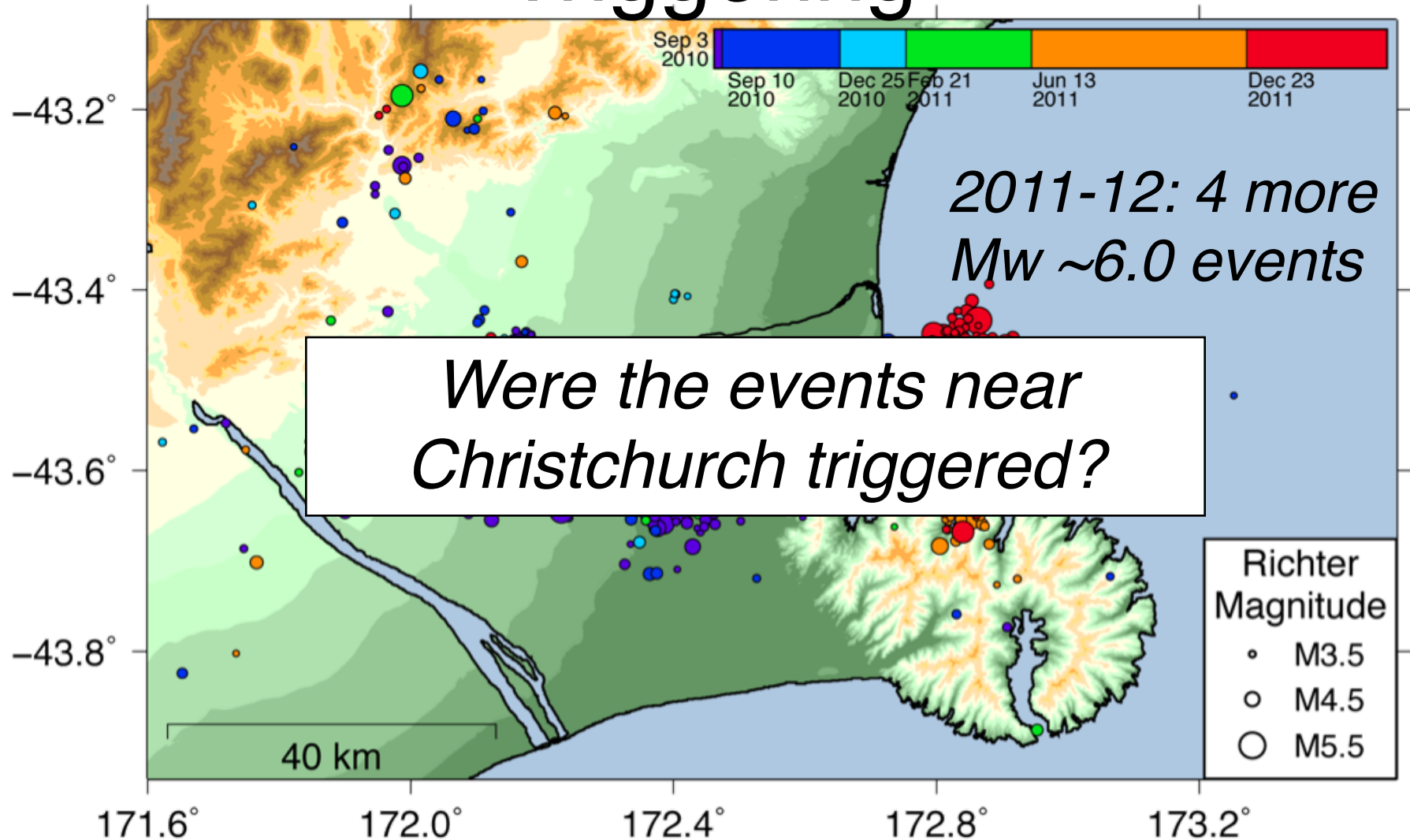
Activity 3: Earthquake Triggering



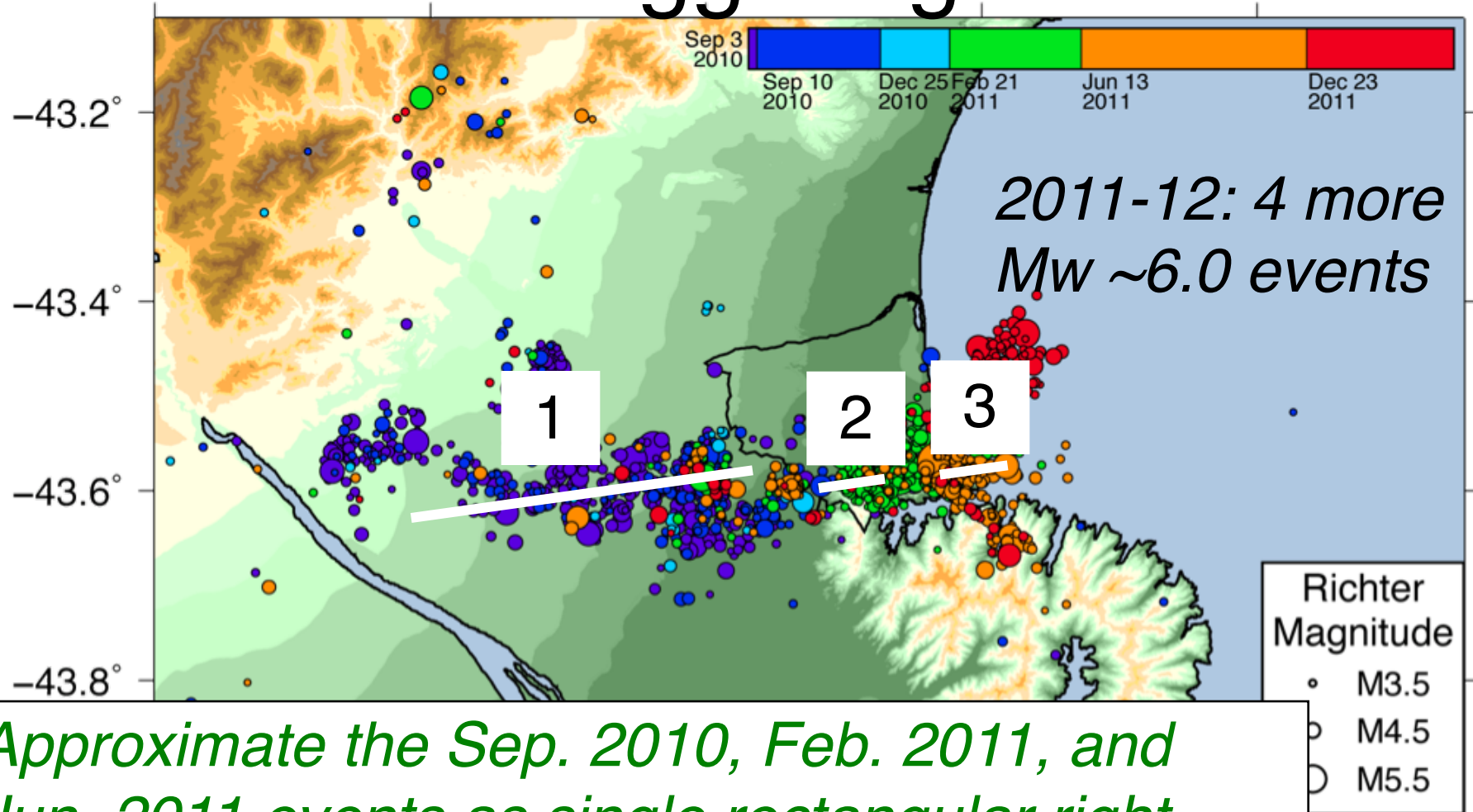
Activity 3: Earthquake Triggering



Activity 3: Earthquake Triggering



Activity 3: Earthquake Triggering



Approximate the Sep. 2010, Feb. 2011, and Jun. 2011 events as single rectangular right lateral strike-slip earthquakes.

Activity 3: Earthquake Triggering

- *Exercise: Compute the ΔCS resulting from the Sep. 2010 main shock on target faults with the same kinematics. Compare the locations of the Feb. and Jun. 2011 earthquakes with the ΔCS distribution.*

Activity 3: Earthquake Triggering

- Sep. 2010 Mw 7.0

172.20 -43.63 15 80 90 180 2 15 35

- Feb. 2011 Mw 6.1

172.60 -43.60 15 80 90 180 1 6 8

- Jun. 2011 Mw 6.0

172.77 -43.58 15 80 90 180 1 4 6

Activity 3: Earthquake Triggering

- Sep. 2010 Mw 7.0

fault.dat

172.20	-43.63	15	80	90	180	2	15	35
--------	--------	----	----	----	-----	---	----	----

- Feb. 2011 Mw 6.1

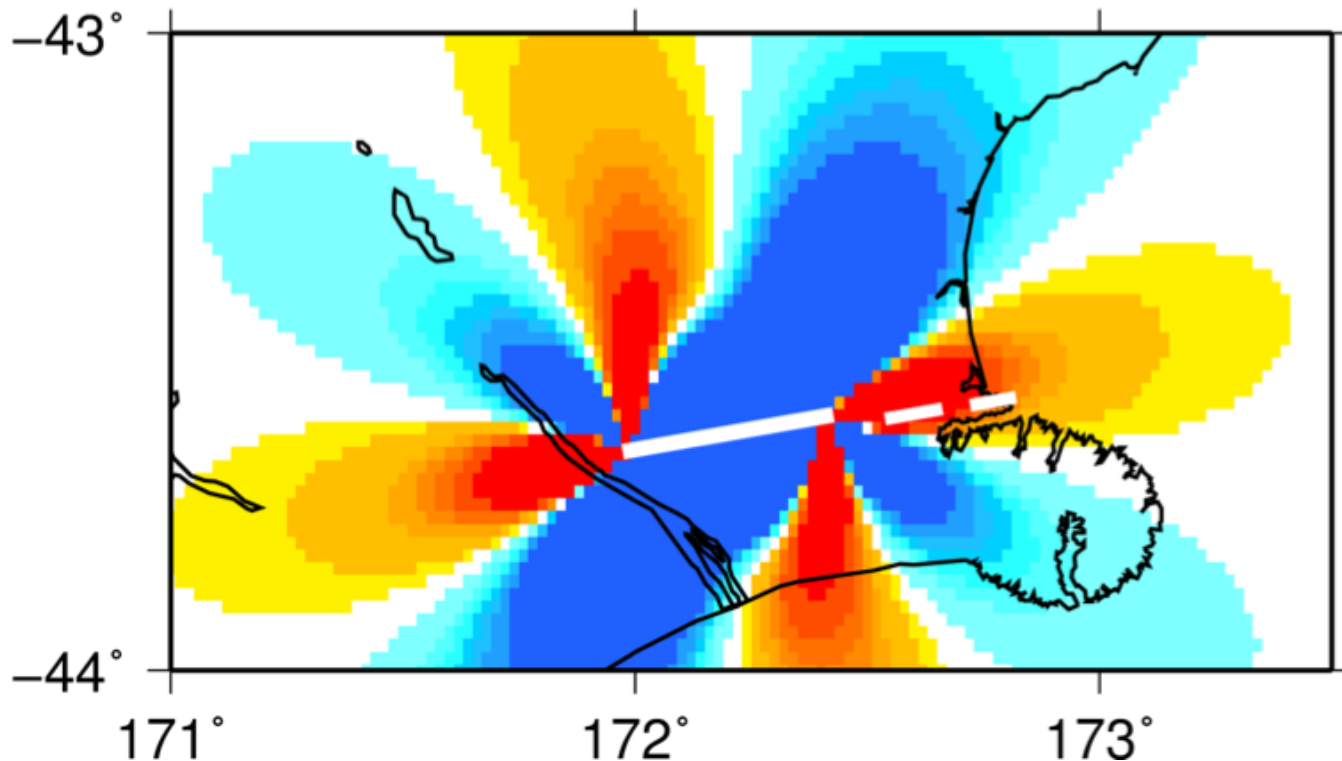
172.60	-43.60	15	80	90	180	1	6	8
--------	--------	----	----	----	-----	---	---	---

- Jun. 2011 Mw 6.0

172.77	-43.58	15	80	90	180	1	4	6
--------	--------	----	----	----	-----	---	---	---

Activity 3: Earthquake Triggering

- Sep. 2010 Mw 7.0 earthquake puts the east in a lobe of positive ΔCS



Activity 3: Earthquake Triggering

- NOTE: The color scheme is chosen with the following criteria:
 - The ΔCS colors saturate at ± 0.1 MPa. Anything larger than this is considered a very large stress change.
 - The minimum colored value is ± 0.01 MPa (0.1 bar). Past studies indicate this is a minimum ΔCS threshold correlated with increased seismicity.

Activity 3: Earthquake Triggering

- *Add the ΔCS resulting from the Feb. 2011 aftershock to the Sep. 2010 main shock ΔCS and see what effect this has on the distribution of ΔCS .*

Activity 3: Earthquake Triggering

- Sep. 2010 Mw 7.0

fault.dat

172.20	-43.63	15	80	90	180	2	15	35
--------	--------	----	----	----	-----	---	----	----

- Feb. 2011 Mw 6.1

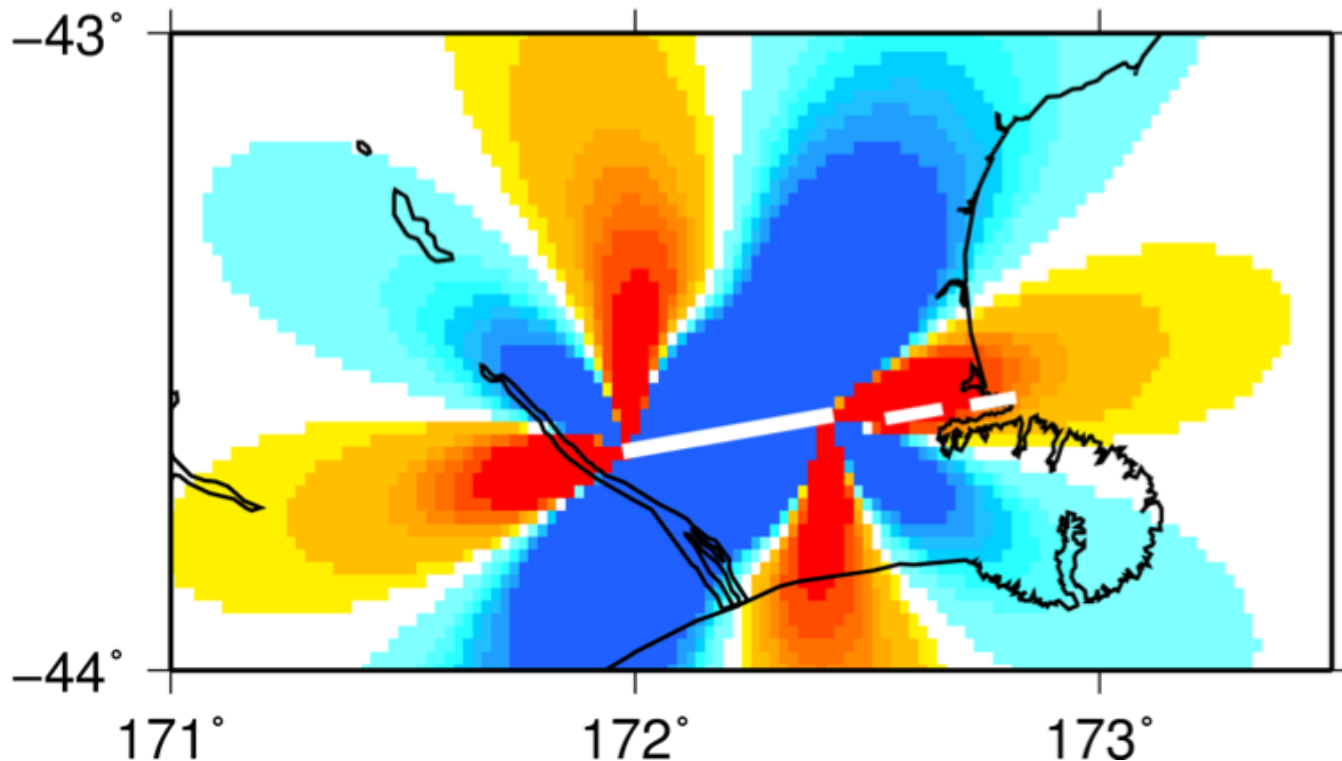
172.60	-43.60	15	80	90	180	1	6	8
--------	--------	----	----	----	-----	---	---	---

- Jun. 2011 Mw 6.0

172.77	-43.58	15	80	90	180	1	4	6
--------	--------	----	----	----	-----	---	---	---

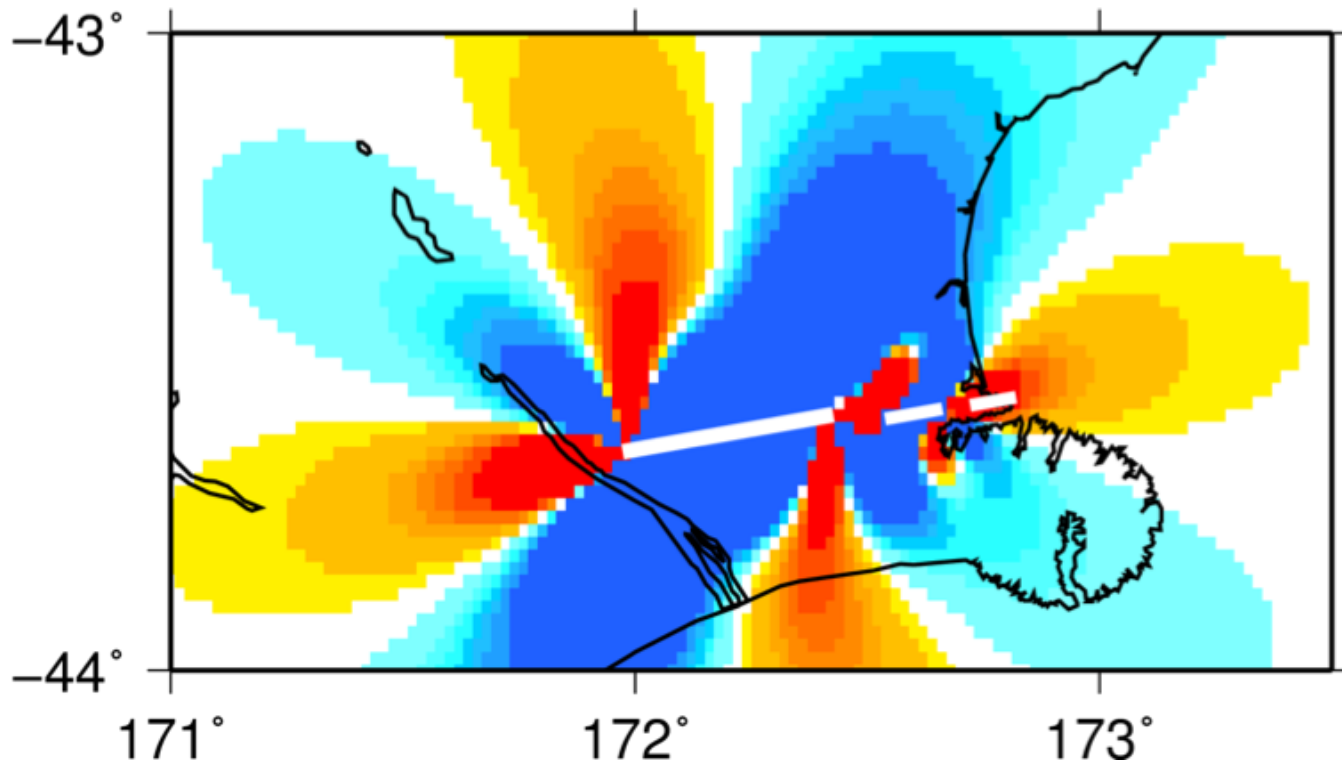
Activity 3: Earthquake Triggering

- Sep. 2010 Mw 7.0 earthquake puts the east in a lobe of positive ΔCS



Activity 3: Earthquake Triggering

- Feb. 2011 Mw 6.1 extends a lobe of positive ΔCS to the June epicenter.



Activity 3: Earthquake Triggering

- *What is the final distribution of ΔCS after all three earthquakes?*

Activity 3: Earthquake Triggering

- Sep. 2010 Mw 7.0

fault.dat

172.20	-43.63	15	80	90	180	2	15	35
--------	--------	----	----	----	-----	---	----	----

- Feb. 2011 Mw 6.1

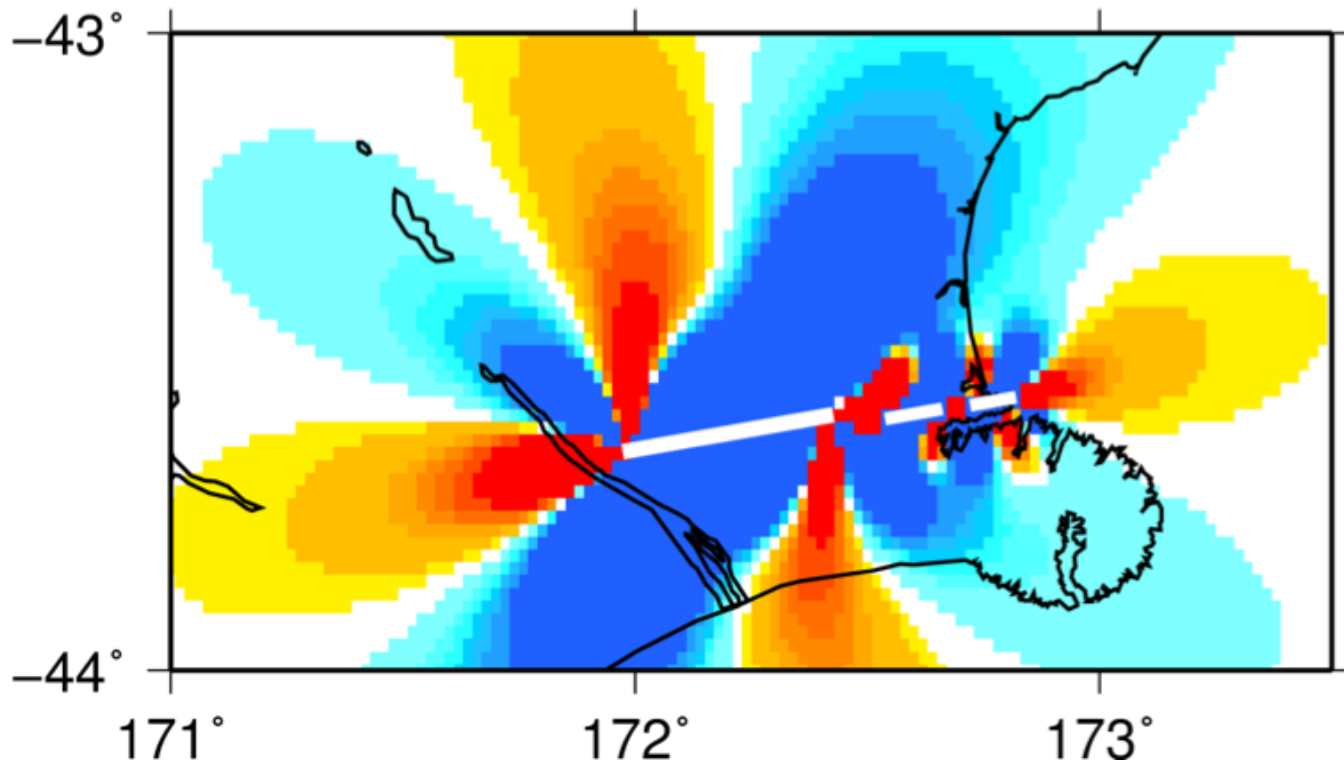
172.60	-43.60	15	80	90	180	1	6	8
--------	--------	----	----	----	-----	---	---	---

- Jun. 2011 Mw 6.0

172.77	-43.58	15	80	90	180	1	4	6
--------	--------	----	----	----	-----	---	---	---

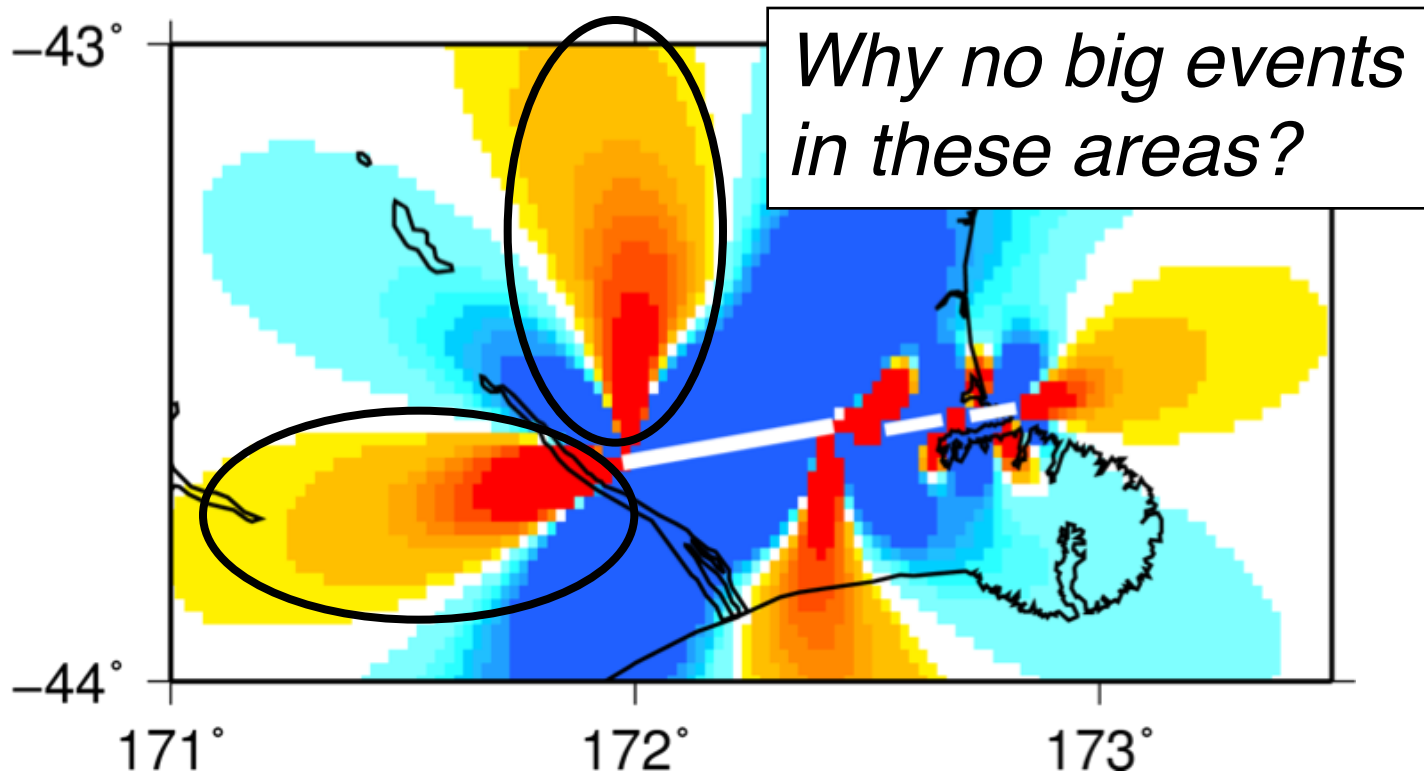
Activity 3: Earthquake Triggering

- Final ΔCS picture after all three earthquakes



Activity 3: Earthquake Triggering

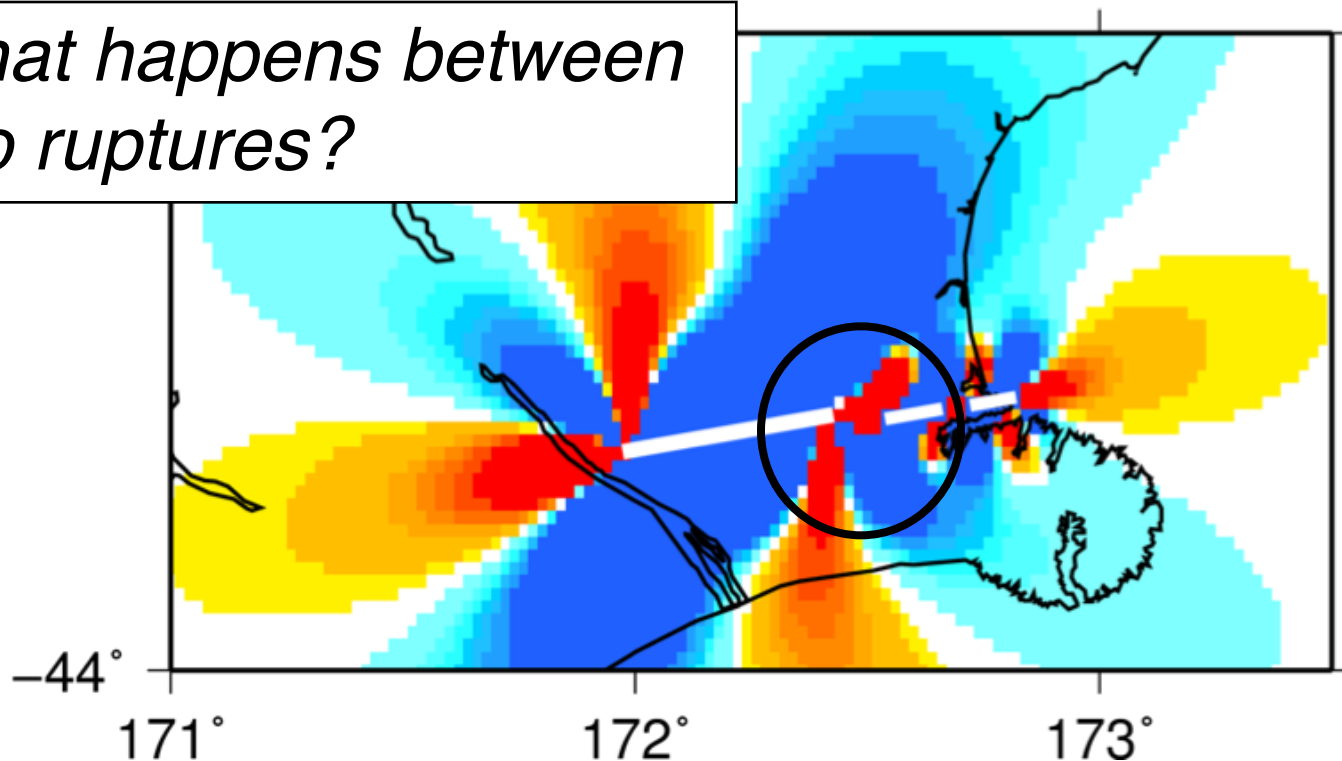
- Final ΔCS picture after all three earthquakes



Activity 3: Earthquake Triggering

- Final ΔCS picture after all three earthquakes

What happens between two ruptures?



Resolving Stress Components and Earthquake Triggering Completed